

B.Sc. COMPUTER SCIENCE-SEMESTER - III DATA STRUCTURES AND ALGORITHMS

UNIT -I

Algorithms (Analysis and design): Problem solving - Top-Down and Bottom- up approaches to algorithm design - Use of algorithms in problem solving - Design, Implementation, Verification of algorithm - Efficiency analysis of algorithms: Space, Time complexity, and Frequency count - Sample algorithms: Exchange the value of two variables - Summation of set of numbers - Decimal to Binary conversion - Sorting - Factorial - Fibonacci - Finding a largest Number in an array - Reverse the order of elements in array.

UNIT-II

Introduction: Definitions - concepts - Overview - Implementation of Data Structures. Arrays: Definition - Terminology - One dimensional array - Multi Dimensional Array. Stacks: Introduction - Definition - Representation of stacks - Operations on stacks - Applications of stack: Evaluation of Arithmetic Expression- Implementation of Recursion- Factorial Calculation

UNIT –III

Queues: Introduction - Definition - Representation of Queues - Various Queue Structures: Circular Queue - De-queue - Priority Queue - Applications of Queues: CPU Scheduling. Linked List: Definition - Single Linked List - Double Linked List - Circular Double Linked List - Applications: Sparse Matrix - Polynomial.

UNIT-IV

Trees: Terminologies - Definitions &Concepts - Representation of Binary tree - Operations on Binary Tree - Types of Binary Trees: Expression Tree - Binary Search Tree - Heap Tree - Red Black Tree. Graphs: Introduction - Graph terminologies - Representation of Graphs - Operations on Graphs - Applications of Graph: Shortest path problem - Minimum Spanning Tree: Kruskal and Prims Algorithm.

UNIT- V

Searching: Terminologies - Linear Search techniques with - Array, Linked List, and Ordered List -Binary search - Non Linear Search- Binary Tree Searching - Binary Search Tree Searching .Sorting: Terminologies - Sorting Techniques - Insertion Sort - Selection sort - Bubble sort - Quick sort -Merge sort.

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TEXT BOOKS

- Sathish Jain, Shashi Singh, "Data Structure Made Simple", 1st Edition, BPB Publications, New Delhi, 2006.
- 2. Debasis Samanta, "Classic Data Structures", 2nd Edition, PHI Learning, New Delhi, 2009.

REFERENCE BOOKS

- 1. Aprita Gopal, "Magnifying Data Structures", 1st Edition, PHI Learning, New Delhi, 2010.
- 2. Chitra A & Rajan PT, "Data Structures", 2nd Edition, Vijay Nicole Publications, 2016

UNIT-I

ALGORITHMS (ANALYSIS AND DESIGN)

PROBLEM SOLVING

- To solve a problem using computer to write step by step solution first and write simple instructions for each operation.
- \blacktriangleright There might be a number of methods to solve the problem.

These steps are:

- > Formulating the problem and deciding the data types to be entered.
- > Identifying the steps of computation that are necessary for getting the solution.
- Identifying decision points.
- ➢ Finding the result and verifying the values.

Procedure for Problem Solving:

- Problem solving is a logical process of breaking down the problem into smaller parts each of which can be solved step by step to obtain the final solution.
- > Step by step to obtain the final solution.

Six basic steps in solving a problem are:

- ➢ First spend some time in <u>understanding the problem</u>. This means try to formulate a problem correctly.
- Construct <u>a list of variables</u> that are needed to find the solution of the problem.
- Decide the layout for the <u>output.</u>
- Select a programming method best suited to solve the problem and then only carryout the coding using a suitable programming language.
- > <u>Test the program</u>. Select test data so that each part of the program would be checked for correctness.
- Finally use <u>data validation</u> steps to guard against processing of wrongly inputted data.

1) Understanding the Problem:

- Read each statement of the problem slowly and carefully by understanding the keywords.
- > Use paper and pencil to solve the problem manually for some test data.
- **Ex:** Accept a value n and find the sum of first N even integers.

Solution:

- > To take an input value, say a number 6 is given as the value of N.
- Next get the 6 integer values.
- > The first 6 even integers are 2, 4, 6, 8, 10, and 12.
- \succ The sum is 42.
- \checkmark Hence the solution is to be made the sum of first 6 even integers.

2) Construction of the list of variables:

- \blacktriangleright The names chosen for the variables should be an aid to memory.
- > The variables may be I, SUM and COUNT as given below:
 - Generate even integers 2, 4, 6.... (I)
 - Total the sum of even integers 2+4+6.... (SUM)
 - Count the number of even integers 1, 2, 3.... (COUNT)
- Finally 4 variables for this problem is
 - N : To be entered by the user
 - : To generate even integers
 - COUNT: To keep the number of even integer that has been summed.
 - SUM : An accumulator that will hold the current total value of even integers.

3) Output design:

Ι

> The output report should be easily understandable by a reader.

Ex: No of first even integer's Total sum

- 42
- > The output format should have the following characteristics
 - Attractive

6

- Easy to read and
- Self-explanatory

4) Program Development:

- > Draw a flowchart for the procedure for the steps 1, 2 & 3.
- Standard symbols should be used for drawing a flow chart, Then draw a flowchart for each part separately and combine them together using connectors.



5) Testing the program:

- \triangleright Next run the program.
- This means by giving known values to the variables and by checking the result and thus comparing results with manually calculated values.

6) Validating the program:

- > The user of your program may enter values, which are not expected by the program.
- Such values should be rejected by the procedure drawn by you, this known as validation of data.

TOP DOWN AND BOTTOM UP APPROACHES TO ALGORITHM DESIGN

<u>1. Top- Down approach of problem solving:</u>

- Top down design is the technique of breaking down a problem into various sub tasks needed to be performed.
- > Each of these tasks is further broken down into separate subtasks and so on.
- The entire solution of the problem modules and joining them together will make the complete task of solving the complex problem.

- ➢ In top down design we initially describe the problem we are working with at the highest or most general level.
- All the operations at this level and individually break them down into simpler steps that begin to describe how to accomplish the tasks.
- > Top-down process involves working from the most general form, down to the most specific form.



Fig: Top-Down modular design

Advantages of Top-Down approach:

- This approach allows analyst to remain "on top of "a problem and view the developing solution in the context.
- > The solution always proceeds from the **highest level to the lowest level**.
- At each stage in the development the individual operation will be split up into a number of elementary steps.
- > By dividing the problem into a number of sub problems, it is easier to share problem development.
- > Bugs and debugging time grows quickly when the program is long.
- > Top-down characteristic helps in faster completion of the solution of the complex problem.
- Increased comprehension of the problem.
- > Unnecessary lower-level details are removed.
- Reduced debugging time.

2. Bottom-Up approach of problem Solving:

- A large and complex problem it may be difficult to solve.
- It may be easier to solve parts of the problem individually, taking the easier aspects first and thereby gaining the insight and experience to tackle the more difficult tasks, and finally join each of the solutions together to form the complete solution.

Disadvantages:

- > There may be a lack of consistency among modules and thus more reprogramming may have to be carried.
- > Parts of the solutions or programs may not fit together easily.

USE OF ALGORITHMS IN PROBLEM SOLVING

- Algorithm is a step-by-step procedure, which defines a set of instructions to be executed in a certain order to get the desired output.
- If the algorithm is written in a language that the computer can understand then such a set of instructions is called a program.

Rules:

- > The starting point can be implemented.
- More than one starting point would create confusion about where to start, violating the ordering condition just stated.
- Accept to identify one or more of the steps in the algorithms as terminators.
- The characteristic of algorithms is that each individual operation must be both effective and well defined.
- Effective means some formal method must exist for carrying out that operation and also getting an answer.

Developing an Algorithm:

The errors they discover will usually lead to insertions, deletions or modifications in the existing algorithm.

Characteristics of Algorithmic Language:

- Unambiguous Algorithm should be clear and unambiguous. Each of its steps (Or phases), and their inputs/outputs should be clear and must lead to only one meaning.
- ▶ **Input** An algorithm should have 0 or more well-defined inputs.
- Output An algorithm should have 1 or more well-defined outputs, and should match the desired output.
- **Finiteness** Algorithms must terminate after a finite number of steps.
- **Feasibility** should be feasible with the available resources.
- Independent An algorithm should have step-by-step directions, which should be independent of any programming code.

Ex:

To find the sum of the first K integers

Begin

```
read k

if k<=0

then

Write "illegal values for k"

End

else

set i to 1

set sum to 0

repeat k times

add i to sum

increment i by 1

end of the repeat loop

write "the sum of first ", k, "integer is ", sum
```

End.

DESIGN OF ALGORITHMS

- > An algorithm is set of simple instructions to be followed to solve a problem.
- > Each of the algorithms will involve a particular data structure.
- A data structure including the type of data and the frequency with which various operations on data are applied.

How to design an algorithm?

- > Algorithm design is a creative activity. Some common approaches for designing algorithms are
- ✓ Greedy algorithm:
 - The greedy algorithm works in steps.
 - In each step this algorithm selects the best available option until all options finish
 Ex: Shortest path algorithm
- ✓ Divide and Conquer:
 - When the method is applied it often leads to a large improvement in time complexity.
 - A big problem is divided into same type of smaller problems
 - Ex: Quick sort

✓ Non-recursive Algorithm:

- A set of instructions that perform a logical operation can be grouped together as a function.
- If a function, which in turn invokes the calling function, then the technique is called as indirect recursion.

✓ **Randomized algorithm:**

- We can use the feature of random number instead of a fixed number. It gives different results with different input data.
- ✓ Back track algorithms:
 - An algorithm technique to find solutions by trying one of several choices if the choice proves incorrect, computation back tracks or restarts at the point of choice and tries another choice.
 - A back tracking algorithm is to write a function or procedure which traverse the solution space.

Ex: Game tree.

✓ Modular programming approach:

- The importance of splitting a problem into a series of self contained modules that becomes important.
- A module should not exceed about 100 or 50 lines and should preferable be short enough to be on a single page.
- The analysis of an algorithm provides information that gives us a general idea of how long an algorithm will take for solving a problem.

IMPLEMENTATION OF ALGORITHM

After spelling out completely and precisely the requirements for each tasks and sub-tasks, it is time to code them into our programming language once the specification at the top levels are complete and precise, we should code the subprograms at these levels and test them appropriately.

VERIFICATION OF ALGORITHM

- > Verification of algorithm would consist of determining the quality of the output received.
- ➢ It is a process of measuring the performance of the program with any laid down standards. Algorithm verification should precede coding of the programmer.

EFFICIENCY ANALYSIS OF ALGORITHM

- An algorithm analysis provides information that gives us an idea of how long an algorithm will take for solving a problem.
- A number of algorithms might be able to solve a problem successfully yet the analysis of algorithm gives us the scientific reason to determine which algorithm should be chosen to solve the problem most efficiently.

(i) Space complexity:

- Space complexity of a program is the amount of main memory in a computer.
- ➢ It needs to run for completion.
- > The space needed by a program is the sum of the following components:
 - ✓ Fixed part that includes space for the code, space for simple variable and fixed size component variables as well as, space for constant etc.
 - ✓ Variable part that consist of the space needed by component variable whose size is dependent on the particular problem instance being solved and the stack space used by recursive procedure.

(ii) Time complexity:

- Time complexity of a program is the amount of computer time it needed to run a program completion. The time complexity may give time for
 - ✓ Best case
 - ✓ Worst case
 - ✓ Average case

Best case:

- > The algorithm searches the elements in first time itself.
- > Best case takes shortest time it executes as it causes the algorithms to do the least amount of work.

Worst case:

In worst case find the element of time at the end of the total time taken when searching elements fails.

Average case:

- Analyzing the average case behaviors of an algorithm is more complex than best case and worst case.
- ▶ As the volume of data increases, average case of algorithm behaves like worst case algorithm.

(iii) Frequency count:

To make an analysis machine independent it can be assumed that every statement will take the same constant amount of time for it execution.

The time complexity can also expressed to represent by the frequency counts. One such notation for frequency count is order notation ('O' notation)

'O' notation: 'O' notation is used to **measure the performance of any algorithm**. Performance of an algorithm **depends upon the volume of input data.**

- O (1) to mean a computing time that us a constant.
- O (n) is called linear, when all the elements of the linear list will be traversed.
- O (log n) is when we divide linear list to half each time and traverse the middle element.
- O (n log n) is when we divide list half each time and traverse that half portion

SAMPLE ALGORITHMS

(i) Exchanging the value of two variables:

- > Exchanging the value of two variables means interchanging their values.
- \succ Two variables x and y.
- > To swap or interchange the value of x and y.
- Original values of x and y are

Algorithm:

- > Begin
- Get the values of variables x and y
- Assign the value of x to t.
- Assign the value of y to x. So x has original value of y now in place of the original value of x.
- Assign the value of t to y.
- Show the values of x any y
- > Stop

ii) Summation of a set of numbers:

- It is like adding numbers given in series. Computer can add two numbers at a time and retuen the sum of two numbers.
- To Add N numbers, we initialize the variable location S, where to store sum, S=0.
- $S=S+a_1$ where a_1 is the first number
- $S=S+a_2$ (the new value of S contains $a_1 + a_2$)
- $S=S+a_2+a_3$ (the new value of S contains $a_1 + a_2 + a_3$)
- So till $S=S+a_n$

Algorithm:

- 1. Begin
- 2. Read n numbers to be summed
- 3. Initialize sum as 0
- 4. Initialize count as 1
- 5. While count is < or = to n numbers to be added, repeatedly do:
 - a. Read the number at position count, when count is 1 read 1st number, when count is 2, read second number and so on.
 - b. Update the current sum by adding to it the number read.
 - c. Add 1 to count
- 6. Write the sum of n numbers. (after the number at nth count has been added, the control will shift to step 7).
- 7. stop

iii) Reversing Digits of an Integer Number:

Reversing digits basically means changing the digits order backwards.

Input : 1980

Output: 0891

Algorithm:

- ✓ Begin
- \checkmark Get positive integer number to be reversed.
- \checkmark While the integer number being reversed is greater than 10 repeatedly do:
 - Extract the right most digit of the number to be reversed by remainder function ie) function mod(
).
 - ✓ Construct the reversed integer by writing the extracted digit to right hand side of the current reversed number

✓ Write the integer to the RHS of the reversed number

✓ stop

iv) Factorial of a given number:

The product of all positive integers from 1 to n is called the 'factorial n' or 'n' factorial. It is denoted by n!

5! = 1*2*3*4*5 =120

Where n is a + ve integer

Algorithm:

- ✓ Begin
- \checkmark Get the number of which the factorial is to be calculated ie) n.
- ✓ Assign the value of i=1 and factorial =1
- ✓ Calculate factorial n=factorial (n-1) *i
- ✓ Increment the value of I by 1 ie) i=i+1
- ✓ Repeat steps 4 & 5 till step 4 has been executed with the value of i=n
- \checkmark Write the value of factorial
- ✓ Stop.

v) Organize numbers in order (sorting):

_	<u> </u>				· · · · · · · · · · · · · · · · · · ·						
		Sorting of	of numb	ers mea	ins to arr	ange a g	given set	of num	bers in	ascending or in descending order	er.
I	nput:		50	60	10	8	1	6	12		
C	Output	:	1	6	8	10	12	50	60		
		-									

Algorithm:

- 1. Begin
- 2. Read numbers and store them in an array of n elements i.e.) size of array a is n with elements as a[1],a[2],a[3],....a[n].
- 3. Find the smallest element within unsorted array.
- 4. Exchange i.e.) swap smallest value of the array element and store it in 1st element of the unsorted part of array.
- 5. Repeat steps 3 and 4 until all the elements in the array are arranged in the ascending order

6. Stop.

RECURSION

- A recursion function is a function that calls itself to perform a specific operation.
- > The process of a function calling itself is known as recursion.
- > Indirect recursion occurs when one function calls another function that then calls the first function.

Ex: 1

Find the factorial values for the values 1 to 5

```
#include (stdio.h>
int factorial( int value)
{
    if (value = = 1)
        return(1);
    else
        return (value * factorial (value -1));
    }
    void main(void)
    {
        Int I;
        For (i=1; i<=5; i++)
            Printf( "The factorial of %d is %d \n", i, factorial (i));
    }
}</pre>
```

Ex: 2

Using recursion to complete the sum of integers from 1 to n

Int sum(n) Int n;

{

If(n<=1) return n;

Else

```
Lise
```

```
return (n+sum(n-1));
```

}

Question Bank Unit –I

One word question and answers

- 1. A natural number 1 is also a
 - a. Prime number b. real number c. integer number d. none of these
- 2. Prime number is a number
 - a. Divisible by 1 b. Divisible by 1 and by itself c. Divisible by 1 and by itself except the number 1
 - b. None of the above
- 3. Swapping of two numbers is done by
 - a. Direct by interchanging their values with each others
 - b. Storing the value of one in a temp variable and shifting the value of the other into the first and then copying the value of temp to the other
 - c. Transfer one number to other number without storing any number in the temp variable
 - d. None of the above.
- 4. Sorting an array in the ascending order of numbers is the process of
 - a. Putting the largest number first and smallest in the last
 - b. Putting the smallest number first and the largest number in the last
 - c. Putting the numbers in any way you desire
 - d. None of the above
- 5. The product of n natural numbers from 1 to n is called
 - a. a. N! b. n and p c. p and n d. none of the above
- 6. In analysis of algorithm, approximate relationship between the size of the job and the amount of work required to fo it is expressed by using:
 - a. Order of magnitude b. central tendency c. differential equation d. none of these
- 7. Which is better computing time?

a. O(N) b. $O(N^2)$ c. $O(\log N)$ d. none of these

- 8. Modular programming uses
 - a. Only top-down b. only bottom-up method c. both a & b d. none of these
- 9. A step- by -step process is called
 - a. Flowchart b. program c. algorithm d. none
- 10. A program calling itself is called
 - a. Factorial b. Fibonacci series c. GCD d. none

Answers:

1. C 2. C 3. B 4. B 5. A 6. A 7. C 8. C 9. C 10. B

5 Marks

- 1. What is data-structure? What are various data-structures available?
- 2. What is algorithm? Why we need to design an algorithm?
- 3. How will you understand a problem?
- 4. How will you define a problem?
- 5. What is top-down approach? Write advantages of it.
- 6. What is bottom-down approach? Write advantages of it.
- 7. How will you develop an algorithm?
- 8. What is space complexity?
- 9. What is time complexity?
- 10. Write an algorithm for exchange two variables?
- 11. Write an algorithm for Fibonacci sequence.

10 Marks

- 1. Write notes on top-down approach with neat diagram.
- What are the uses of algorithms in problem solving?
 Give a brief notes on efficiency analysis of algorithms.
- 4. Write an algorithm for a) organizing numbers in order b) factorial of a given number.5. Explain in detail about implementation and verification of an algorithm.

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UNIT-II

DATA STRUCTURES

- Data Structure is a way of collecting and organising data in such a way that we can perform operations on these data in an effective way.
- > Data Structures are the programmatic way of storing data so that data can be used efficiently.

Overview of Data Structure:



Categories of data structures:

- i) Linear data structure
 - ii) Non linear data structure

Linear data structure:

In linear data structures processing of data items is possible in linear function (ie, data can be processed One by one).



Linear Data Structure

Ex: Array, Linked list, stack & queue.

Non-linear data structure:

- > The elements do not form a sequence.
- > Insertion and deletion is not possible in a linear function.



Structure

> Ex: Trees and graphs

ARRAYS:

- An array is a collection of two or more adjacent memory locations.
- > The memory location containing same type of data.
- > These memory locations are called array elements which are given a particular symbolic name.
- > Array elements are accessed using their index number.
- > The index number that begins from zero.



Advantages:

- > Insertion and deletion can be done randomly.
- \blacktriangleright At any location, it the start, somewhere at the middle or at the end.

Disadvantages:

> Insertion and deletion operation requires movement of large amount of data.

LINKED LIST

- A linked list is the chain of data items.
- Data items are connected by pointers.
- Each item contains a pointer.
- > The pointer to the address of next item.



Types of linked lists are:

- ✓ Singly linked list
- ✓ Doubly linked list
- ✓ Circular linked list
- ✓ Singly linked list each node contains data and a single link which attaches it to the next node in the list.
- Doubly linked list each node contains data and two links one to the previous node and one to the next node.
- ✓ In circular linked list the last node, instead of pointing to NULL, points to the starting node.

Advantages:

- Quick insertion
- > Quick deletion
- > Insertion and deletion operations in a linked list are much easier

Disadvantages:

➢ Slow search

STACK:

- ➤ A stack is a linear data structure.
- ▶ It is similar to an array.
- Elements are added or removed only from one end of the list.
- ▶ It is also known as **Last-In-First-Out** (**LIFO**).
- > A Stack is implemented as an array or a linked list.



Advantages:

Provide last in first out access.

Disadvantages:

Slow access to other items.

4. QUEUES:

➤ A queue is a linear data structure.

- > Entries can be added or removed at either end but not in the middle.
- > Queue is also known as **First-in- First –Out (FIFO**)
- > Queue is implemented as arrays or linked lists.

Front = 0 Rear		Rear = 2	2					
	10	20	30					
	0	1	2	3	4	5	6	7
Front		Rear				Tutoria	Kus.com	
Delete an Element		Insert a Elemer	ın ıt					

Advantages:

Provides first-in-first-out access

Disadvantages:

Slow access to other items.

Non-linear data structure:

TREE:

- Tree data structure is non-linear data structure.
- A tree is a data structure that represents hierarchical relationships between individual data items.



Figure: Tree data structure

Fig: A tree structure

- > A tree consists of a **collection of nodes** which are connected by directed arcs.
- > A tree contains a unique **first element known as the root**, which is at the top of the tree structure.
- > A node with **no children is called a leaf node**.

> Tree is a very flexible and powerful data structure that can be used for a wide variety of applications. Advantages:

- \checkmark Quick search, insertion and deletion if tree remains balance.
 - \checkmark Easy to understand from the graphical view.

Disadvantages:

 \checkmark Needs unnecessary traversal in order to reach a particular node.

GRAPHS:

- ➤ A graph is a pictorial representation.
- > Set of objects where some pairs of objects are connected by links.
- > The interconnected objects are represented by points termed as vertices.
- > The links that connect the vertices are called edges.
- ➤ Formally, a graph is a pair of sets (V, E).
- ➤ Where V is the set of vertices.
- ➤ E is the set of edges, connecting the pairs of vertices.
- > Take a look at the following graph



Definition:

- A graph is defined as a set of nodes or vertices.
- \succ Set of lines or edges or arcs that connect the two vertices.

Types:

- 1. Undirected graphs
- 2. Directed graphs.

Undirected Graph:

Edges are unordered pairs of vertices.



Directed Graph:

- > A directed graph or digraph, the edges between nodes directionally oriented.
- There are directed edges from A to B, B to C, and C to D & D to E.
- > The directed edges are also called an arc.



Advantages:

- ✓ Graphs are data structures which have wide ranging applications in real life, like analysis of electrical circuits, finding shortest routes, statistical analysis etc.
- ✓ A directed graph is a natural way of describing, representing and analyzing complex projects which consists of may interrelated activities.

<u>ARRAYS</u>

Define array:

- \checkmark It is a linear data structure.
- \checkmark An array is a finite, ordered and collection of homogeneous data elements.
- ✓ It contains only limited number of elements.
- ✓ All the elements are stored one by one in contiguous locations of computer memory in a linear ordered.
- \checkmark All the elements of an array are of the same data type.

Example

Int A [4]; Dim A [4];

ARRAYS TERMINOLOGY:

Size:

> Number of elements in an array is called the size of the array.

> It is also called as **length or dimension**.

Type:

- > Type of an away represents the kind of data type.
- Ex: int, string

Base:

> Base of an array is the address of memory location where the first element in the array is located.

Index:

- All the elements in an array can be referenced by subscript like A_i or A[i], this subscript is known as index.
- Index is always as integer value.
- > Every element is identified by a subscripted or indexed variable.

Range of index:

Indices of array elements may charge from a lower bound (L) to an upper bound (U), which are called the boundaries of an array.

Ex:

Int A [100]: The range of index is from 0 to 99.

A: Array [-5...19] of integer: The points of the rage is -5, -4, -3...18, 19.

Here L is the lower bound.

Formula is Index $(a_i) = L+i-1$

If the range of index varies from L....U then the size of the away can be calculated as Size (A) = U-L+1Word:

- \succ It denotes the size of an element. In memory location computer can store an element of word size w.
- > This word size varies from machine to machine such as 1 byte to 8 bytes.

ONE DIMENSIONAL ARRAY

Definition:

Only one subscript /index is required to reference all the elements in an array then the array will be termed as one dimensional array.



One-dimensional array with six elements

Example:

Declare a variable without using array,

- int mark1;
- int mark2;
- Declare a variable using array,
 - int mark [3];

mark1	mark2
X[0]	X[1]

MEMORY ALLOCATION FOR AN ARRAY

- The memory location where the first element can be stored is M.
- If each element requires one word then the location for any element say A[i] in the array can be obtained as

Address (A[i] = M+ (i-1)

- An array can be written as A[L...,U], where L & U denote the lower and upper bounds for index.
- > If it is stored starting from memory locations and for each element it requires w number of words.
- ➤ Then the address for a[i] will be

Address
$$(A[i]) = M + (i-L) * W$$

> The formula is known as indexing formula which is used to map the logical presentation of an array to physical presentation.

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2. Sorting:

> This operation if performed on an array will sort it in a specified order.

 \succ The algorithm is used to store the elements of an integer array in ascending order.

Input : An array with integer data

Output : An array with sorted element in an order according to ORDER ()

Steps:

 $i= U \\ While i>= L do \\ j=L // start comparing from first \\ While j< i do \\ If ORDER (A[j, A[j+1]) = FALSE // if A[j] and A[j+1] are not in order \\ Swap (A[j], A [j+1]) // Interchange the elements \\ End if \\ j=j+1 // Go to next statement \\ End while \\ i=i-1 \\ End while \\ Stare$

Stop

Here order () is a procedure to test whether two elements are in order and SWAP () is a procedure to interchange the elements between two consecutive locations.

3. Searching:

> This operation is applied to search an element of interest in an array.

Algorithm : Search array (key)

Input : Key is the element to be searched

Output : Index of key in A or a message on failure

Steps:

I=L, found=0, location=0 // found=0 indicates search is not finished and unsuccessful While (i.e. II) and (from 1 = 0) do

While (i<=U) and (found =0) do

If compare (A[i], key) = true then Found=1 Location =i

Else

i=i+1 End if

End while

If found=0 then

Print "search is unsuccessful, key is not in the array "

Else

Print "search is successful: key is in the array at location ", location

End if

Return (location) Stop

4. Insertion:

This operation is used to insert an element into an array provided that the array is not full. Algorithm: insert (key, location)

Input : key is the item; location is the index of the element where it is to be stored.

Output: array enriched with key

Steps:

If A [U] # NULL then

Print "Array is full, no insertion possible" Exit

Else

While i> location do A [i+1] =A[i] i = i-1

```
End while
A[location] =key
U=U+1
```

End if Stop

5. Deletion:

This operation is used to delete a particular element from an array. The element will be deleted by overwriting it with its subsequent element and this subsequent element then is to be deleted.

Algorithm: delete (key)

Input: key is the element to be deleted. Output: slimed array without key Steps: i = search array (a, key)if i = 0 then Print "key is not found, no deletion" Exit Else While i< U do A[i] = A[i+1]i = i + 1End while End if A[U] = NULLU=U-1Stop 6. Merging: Merging is an important operation when we need to compact the elements from two different arrays into a single array. Algorithm: merge (A1, A2: A) **Input:** Two arrays A1 [L1...U1], A2 [l2...U2] **Output:** Result array A [L...U], where L=L1 and U=U1+(U2-L2+1) when A1 is append after A2 Steps: i1=L1, i2=L2; // initialization of variables L=L1, U=U1+U2 -L2 +1 // initialization of lower and upper bounds of an array i=L Allocate memory for a[L...U] // to copy array A1 into the first part of A While i1<U do A[i] = A1[i1]i=i+1, i1=i1+1 End while While i2<=U2 do // to copy the array A2 into last part of A A[i] = A2[i2]i=i+1, i2=i2+1 End while Stop

Application of Array:

Every programming language include this data type as a built in data type.
Ex:

To store records of all students in a class, the record structure is given by students.

ROLLNO	MARK1	MARK2	MARK3	TOTAL	GRADE
(Alphanumeric) (N	Numeric) (Nume	ric) (Numeric)	(Numeric)	(Character)	

If sequential storage of records is not an objection, then we can store the records by maintaining 6 arrays whose size is specified by the total number of students in the class.

ROLLNO MARK1 MARK2 MARK3 TOTAL GRADE

MULTIDIMENSIONAL ARRAYS

Two dimensional Arrays:

- > Two dimensional arrays are the collection of homogeneous elements.
- ▶ It also called matrix.
- > The elements are ordered in a number of rows and columns.

Columns

	2D ARRAY	0	1	2
SW	0	a[0][0]	a[0][1]	a[0][2]
Rot	1	a[1][0]	a[1][1]	a[1][2]
	2	a[2][0]	a[2][1]	a[2][2]

Ex:

- \blacktriangleright An (m x n) matrix where m denotes the number of rows and n denotes the number of columns.
- \succ The subscript of any arbitrary elements say (a_{ij}) represents the ith row and jth column.

Memory Representation of a Matrix:

- > Matrix representation is a method used by a computer language.
- > Used to store matrices of more than one dimension in memory.



Three dimensional arrays:

a



Three-dimensional array with twenty four elements

- Three dimensional arrays have three indexes.
- First index refers to dimension.
- Second index refers to row.
- > Third index refers to column.

Example:



Pointer Array

- Address of memory variable or array is known as pointer and an array containing pointers as its elements is known as pointer array.
- An array of pointers is an indexed set of variables in which the variables are pointers (a reference to a location in memory).

Ex:

To store the marks of all students of computer science & engineering dept for a year, there are six classes, say cs1,cs2.....cs6

STACKS

Introduction

- Stack is a linear data structure.
- > Very much useful in various applications of computer science.
- Stack is a collection of elements in a Last-In-First-out fashion.
- ➢ Stack is also called as LIFO.



Ex:

- \checkmark Shunting of trains in a rail yard.
- \checkmark Shipment in a cargo.
- \checkmark Order supply in a restaurant.
- ✓ Arrangements of books.

Definition

- A stack is an ordered collection of homogeneous data element.
- > Where the insertion & deletion operation take place at one end only.
- Stack is also a linear data structure.
- > The insertion and deletion operations in case of stack are specially termed as PUSH and POP.
- > Where the operations are performed is known as TOP of the stack.
- > An element in a stack is termed as ITEM.
- > The maximum number of elements that a stack can accommodate is termed as SIZE.

REPRESENTATION OF STACK

- A stack representation in two ways
 - 1. Using one dimensional array.
 - 2. Single linked list

Array representation of stacks:

Array Representation of Stack



- Allocate a memory block of sufficient size to accommodate the full capacity of the stack.
- > Then from the first location of the memory block, items of the stack can be stored in sequence mode.
- Item denotes the ith item in the stack, 1 and u denote the index range of array in use, and these values are 1 and size.
- > Top is a pointer to point the position of array up to which it is filled with the items of stack.
- There are two statuses

```
EMPTY: TOP < l
FULL : TOP >= u+l-1
```

Linked list representation of stacks:

- > The size of the stack may vary during program execution.
- Single linked list structure is sufficient to represent any stack.

```
Тор
```



Fig.: 5.4: Linked list representation of a stack

OPERATIONS ON STACKS

```
Basic operation required to manipulate stacks:
```

- (i) **PUSH** To insert n item into the stack
- (ii) **POP** To remove an item from a stack

(i) PUSH algorithm:

Algorithm PUSH_A (ITEM)

Steps:

If TOP > = SIZE then

Print "stack is full"

Else

```
TOP= TOP+1;
A [TOP] = ITEM
```

End if

Stop

Array index varies from 1 to SIZE and TOP points the location of the current top-most item in the stack.

```
(ii) POP Algorithm:
```

Algorithm POP_A ()

Steps:

If TOP < 1 then Print "stack is empty"

```
Else
```

ITEM=A [TOP]

TOP=TOP-1

End if Stop

Next operation is to test the various states of a stack like whether it is full or empty, how many items are right now in it and read the current element at the top without removing it.

Same operations can be defined for a Stack using Linked List:

```
(i) PUSH Algorithm:
Algorithm: PUSH_L (ITEM)
Steps:
new= GETNODE(NODE)
```

```
new.DATA=NEW
new.LINK=TOP
TOP=new
STACK_HEAD.LINK=TOP
Stop
```

(ii) POP Algorithm:

```
Algorithm: POP_L ()
Steps:
If TOP = NULL
```

print " stack is empty" Exit

Else

End if Stop

```
ptr =TOP.LINK
ITEM= TOP.DATA
STACK_HEAD.LINK=ptr
TOP=ptr
```

APPLICATIONS OF STACK

- \checkmark A classical application deals with evaluation of arithmetic expression; compiler uses a stack to translate input arithmetic expression into their corresponding object code.
- ✓ Some machines are also known which use built-in-stack hardware called "stack machine".
- ✓ Another important application of stack is during the execution of recursive program, some programming languages use stacks to run recursive programs.
- ✓ There are two scope rules known Static scope rule and dynamic scope rule.
- ✓ Implementation of such scope rule is possible using stack known as run time stack.

<u>1. Evaluation of Arithmetic Expression:</u>

- An arithmetic expression consists of operands and operators.
- Operands are variables or constant and operators are of various types like arithmetic unary and binary operators (+, -, Unary, *, /, ^, %) and relational operators (<, <=, >, >=, <>) and Boolean operators (AND, OR, NOT, XOR).
- > A simple arithmetic expression is

A+B

- > The problem to evaluate this expression is the order of evaluation.
- ➤ There are two ways to fix it

Operators	Precedence	Associativity
(-) Unary, + (Unary), NOT	6	-
^ (Exponentiation)	6	Right to Left
*, /	5	Left to Right
+, -	4	Left to Right
<, <=, +, >=, <>	3	Left to Right
AND	2	Left to Right

OR, XOR	1	Left to Right

Notations for arithmetic expressions:

- > There are 3 notations to represent an arithmetic expression infix, postfix and prefix.
- > The conventional way of writing an expression is called infix.

Ex:

A +B, C-D, E * F, G/H etc

Infix notation:

- \succ The notation is
 - < Operand> <operator> <operand>
- > This is called **infix** because the operators come in between the operands.

A +B

Prefix notation:

 \blacktriangleright The prefix notation on the other hand user the conventions.

<Operator> < Operand> <operand>

> The operator comes before the operands.

+AB

This notation was introduced by polish mathematician Jan Lukasiewicz and hence also termed as polish notation.

Postfix notation:

> The last notation is called the postfix (or) suffix notation where operators is suffixed by operands.

< Operand> < operand> < operator>

AB+

- This notation is just reverse to the polish notation; hence it is also alternatively termed as reverse polish notation.
- An expression given in infix notation can be easily converted into its equivalent prefix or postfix notation.

Rules for convert and infix expression into a postfix form:

- > Assume the fully parenthesized version of the infix expression.
- > Move all the operators so that they replace their corresponding right part of parentheses.
- ➢ Remove all parentheses.

Ex:

Arrows point from operators to its corresponding right parenthesis

(A*(B+(C/D))))

Operators are moved to their respective right parenthesis.

Output:

(A(B(CD/)+)*)

Three notations for the given arithmetic expression:

Infix: (A * (B + (C/D)))

Prefix: (*(+(/CD)B)A)

Postfix: (A (B (CD/)+)*)

- ✓ In both the prefix and postfix equivalents of an infix expression, the variables are in the same relative positions.
- \checkmark The expressions in prefix or postfix form are completely parenthesis free.
- \checkmark The operators are rearranged according to the rules of precedence of operators.
- ✓ Out of three notations, postfix notation has certain advantages over other notations from the computational point of view.
- \checkmark The main advantage is its evaluation.
- ✓ During the evaluation of an expression in postfix notation it no more requires to scan the expression from left to right several times, but exactly once.

Conversion of an infix expression to postfix expression:

- A simple arithmetic expression containing +, -, *, / and ^ operators only.
- > The expression may be parenthesized or unparenthesized.

First we have to append the symbol ')' as delimiter at the end of a given infix expression and initialize the stack with '('.

Symbol	In stack priority	In coming priority values
+-	2	1
* /	4	3
^	5	6
Operand	8	7
(0	9
)	-	0

There are two priority values

✓ In stack priority

✓ In coming priority values

- ➤ A symbol will be pushed on to the sack if its incoming priority value is greater than the in-stack priority value of the top-most element.
- Similarly a symbol will be popped from the stack if its in-stack priority value is greater that the instock priority value of the top-most element.
- Similarly a symbol will be popped from the stack if its in-stack priority value is greater or equal to the incoming priority value of the in-coming element.

Function:

READ-SYMBOL () - From a given infix expression this will read the next- symbol. ISP(X) – Returns the in-stack priority value for a symbol x ICP(X) – Returns the incoming priority value for a symbol x OUTPUT(X)- Append the symbol x into the resultant expression.

```
Algorithm: INFIX-TO-POSTFIX (E)
Steps:
   TOP=0, PUSH ('(')
   While (TOP > 0) do
          item = E.READ-SYMBOL()
          x = POP()
          case: item=operand
                   PUSH(X)
                   OUTPUT (ITEM)
          case: item= ')'
                     While x # '('do
                            OUTPUT(X)
                            X=POP()
                     End while
          case: ISP(X) > = ICP(ITEM)
                     While (ISP(X) \ge ICP (ITEM)) DO
                            OUTPUT(X)
                            X=POP()
                     End while
                     PUSH(X)
                     PUSH (ITEM)
          case: ISP(X) < ICP(ITEM)
                     PUSH(X)
                     PUSH (ITEM)
          Otherwise: print "invalid expression"
End while
Stop
```

Ex: Infix form (A+B) ^ C-(D*E)/F) Symbol reading 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

Read symbol	stack	output
Initial	(
1	((
2	((А
3	((+	А
4	((+	AB
5	(AB+
6	(^	AB+
7	(^	AB + C
8	(-	AB + C ^
9	(- (AB + C ^
10	(- ($AB + C^{D}$
11	(- (*	$AB + C^{D}$
12	(- (*	$AB + C^{DE}$
13	(-	$AB + C \wedge DE *$
14	(- /	AB + C ^ DE *
15	(- /	AB + C ^ DE * F
16		AB + C ^ DE * F / -

Output: A B + C ^ DE * F / - (postfix form)

EVALUATION OF POSTFIX EXPRESSION:

```
> Algorithm EVAL_POSTFIX is to evaluate an arithmetic expression in postfix notation using a stack. Steps:
```

```
Append special delimiter '# at the end of the expression
item = E.READ_SYMBOL() // Read the first push into the stack
While (item = "\#") do
     If (item = operand) then
                                    // Operand is first push into the stack
     PUSH (item)
     Else
                                    // The item is an operator
     op = item
     y = POP()
                                    // The right most operand of the current operator
                                    // The left most operand of the current operator
     x = POP()
                                    // Perform the operation with operator 'op' and operand x,y
     t = x op y
     PUSH (t)
                                    // Push the result into stack
     End If
     Item = E.READ SYMBOL () // Read the next item from E
End While
                                             // Get the value of the expression
Value = POP()
```

```
Return (value)
Stop
```

Example:

Infix: A + (B * C) / D Postfix: A B C * D / + Input: A B C * D / + # with A = 2, B = 3, C = 4, and D = 6

ALGORITHM FOR CONVERTING A POSTFIX EXPRESSION:

```
Algorithm POSTFIX_TO_CODE (E)
Input: An arithmetic expression E in postfix notation
Output: Assembly code.
Steps:
       Append delimiter '#' at the end of the expression
       item=E.READ_SYMBOL()
       i=1, TOP=0
       While (item \neq '#') do
               case: item =operand
               PUSH (item)
               case: item='+'
                       X=POP()
                       Y=POP()
                       PRODUCE_CODE (Y, X,'ADD', Ti)
                       PUSH (Ti)
           case: item='-'
                       X=POP()
                       Y=POP()
                       PRODUCE_CODE (Y, X, 'SUB', Ti)
                      PUSH (Ti)
           case: item='*'
                       X=POP()
                       Y=POP()
                       PRODUCE_CODE (Y, X,'MUL', Ti)
                       PUSH (Ti)
           case: item='/'
                      X = POP()
                       Y = POP()
                       PRODUCE_CODE (Y, X,'DIV', Ti)
                       PUSH (Ti)
           Otherwise
                       print "Error in input"
                      Exit
           item =E.READ-SYMBOL()
           i=i+1
       End while
       stop
Ex:
       Infix: (A+B) *C/D
```

```
Postfix: AB+C*D/
```

3. IMPLEMENTATION OF RECURSION:

- ➤ A recursion is termed as recursive if the procedure is defined by itself.
- ➢ Factorial of given integer n:

n! = n * (n -1) * (n-2) * * 3*2 *1 or n! =n * (n-1)

```
Algorithm: Factorial (n)
Steps:
```

```
fact =1
for (i=1 to n) do
Fact=i*fact
end for
return (fact)
stop
```

> Here step 2 defines the interactive definition for the calculation of factorial

<u>Algorithm</u>: Factorial (N) // using recursion Steps:

```
if (n=0) then

1. Fact=1

else

1. Fact= n* factorial (n-1)

endif

return(fact)

stop
```

Step 2 recursively defines the factorial of an integer N. This is actually a direct translation of $n! = n^*(n-1)!$ In the form of Factorial (n) = n* factorial (n-1).

4. FACTORIAL CALCULATION:

```
Algorithm: FACTORIAL_STACK(N)
```

Return (fact)

UNIT II Question Bank

On	e word question and answers:	
1.	Which of these best describes an array?	
	a) A data structure that shows a hierarchical behavior b) Container of objects of similar types	
2	C) Arrays are immutable once initialized d) Array is not a data structure Answer: D	
2.	How do you initialize an array in C? a) int $am[2] = (1, 2, 2);$ b) int $am(2) = (1, 2, 2);$ c) int $am[2] = (1, 2, 2);$ d) int $am(2) = (1, 2, 2);$	
	a) Int $an(5) = \{1, 2, 5\};$ b) Int $an(5) = \{1, 2, 5\};$ c) Int $an(5) = \{1, 2, 5\};$ d) Int $an(5) = (1, 2, 5);$	
3	Answer: c What are the advantages of arrays?	
5.	a) Objects of mixed data types can be stored b) Elements in an array cannot be sorted	
	c) Index of first element of an array is 1 d) Easier to store elements of same data type. Answer: d	
4	In general, the index of the first element in an array is	
ч.	a) $(b) -1$ (c) $(c) -1$ (c) (
5	Elements in an array are accessed	
5.	a) randomlyb) sequentially_c) exponentiallyd) logarithmically Answer: a	
6	Process of inserting an element in stack is called	
0.	a) Create b) Push c) Evaluation d) Pop Answer: b	
7	Process of removing an element from stack is called	
<i>.</i>	a) Create b) Push c) Evaluation d) Pop Answer: d	
8.	In a stack, if a user tries to remove an element from empty stack it is called	
	a) Underflow b) Empty collection c) Overflow d) Garbage Collection Answer: a	
9.	Pushing an element into stack already having five elements and stack size of 5, then stack becomes	
	a) Overflowb) Crash c) Underflow d) User flow Answer: a	
10.	Entries in a stack are "ordered". What is the meaning of this statement?	
	a) A collection of stacks is sortable b) Stack entries may be compared with the '<' operation	
	c) The entries are stored in a linked list d) There is a Sequential entry that is one by one	
	Answer: d	
11.	Which of the following applications may use a stack?	
	a) A parentheses balancing program b) Tracking of local variables at run time	
	c) Compiler Syntax Analyzer d) Data Transfer between two asynchronous process Answer: d	
12.	What is the value of the postfix expression $6 3 2 4 + - *$:	
	a) 1b) 40 c) 74 d) -18 Answer: d	
13.	Here is an infix expression: $4 + 3*(6*3-12)$. Suppose that we are using the usual stack algorithm to	
	convert the expression from infix to postfix notation.	_
	The maximum number of symbols that will appear on the stack AT ONE TIME during the conversion of	Эf
	this expression?	
	a) 1b) 2 c) 3 d) 4 Answer: d	
14.	The postfix form of the expression $(A+B)*(C*D-E)*F/G$ is?	
	a) $AB + CD^*E - FG / ^* $ b) $AB + CD^*E - F^*G / $ c) $AB + CD^*E - *F^*G / $	
15	a) $AB + CDE^{*} - F^{*}G/$ Answer: c The data structure required to should whether an expression contains belowed normathesis is?	
15.	a) Steels and a structure required to check whether an expression contains balanced parentnesis is?	
16	a) Stack D) Queue C) Array U) free Allswer: a What data structure would you mostly likely see in a non recursive implementation of a recursive	
10.	algorithm?	
	algonumn: a) Linkad List b) Stack a) Quana d) Traa Answar: b	
17	The process of accessing data stored in a serial access memory is similar to manipulating data on a	
17.	The process of accessing data stored in a serial access memory is similar to manipulating data on a	
	a) Heap b) Binary Tree c) Array d) Stack Answer: d	
18	The postfix form of $A*B+C/D$ is?	
10.	a) $*AB/CD+$ b) $AB*CD/+$ c) $A*BC+/D$ d) $ABCD+/*$ Answer: h	
19.	Which data structure is needed to convert infix notation to postfix notation?	
	a) Branch b) Tree c) Queue d) Stack Answer: d	

20.	The prefix form of A	$A-B/(C * D ^ E)$) is?		
	a) -/*^ACBDE	b) -ABCD*^DE	Ec) -A/B*C^DI	E d) -A/BC*^DE	Answer: c
21.	What is the result of	the following o	peration?		
	Top (Push (S, X))				
	a) X	b) X+S	c) S	d) XS	Answer: a
22.	The prefix form of a	n infix expression	on $(p + q) - (r^{2})$	* t) is?	
	a) + $pq - *rt$	b) $-+pqr * t$	c) - +pq * rt	d) - + * pqrt	Answer: c
23.	Which data structure	e is used for imp	lementing recu	rsion?	
	a) Queue b) Stack	c) Array	y d) Lis	t	Answer: b

5 Marks

- 1. Define array and its basic terminologies.
- 2. Explain in detail about one dimensional array with an example.
- 3. Explain in detail about multi dimensional array with an example.
- 4. Write about memory allocation of an array.
- 5. Write notes on stack representation.
- 6. Explain in detail about evaluation on infix expression.

10 Marks

- 1. Write in detail on representation of an array.
- 2. Give a brief note on operations on stack.
- 3. Write notes on data structure and its types.
- 4. Give a brief note on application of stack.
- 5. Write an algorithm of infix to postfix conversion.
- 6. Write an algorithm for factorial calculation.

_____END OF THE UNIT II _____

UNIT – III

QUEUE

What is Queue?

- > Queue is a simple but very powerful data structure.
- > Solve numerous computer applications.
- ➢ It is Linear Data Structure.
- Insert element at one end called Rear. \triangleright
- Delete element at another end called Front.

Front = 0 Rear = 2



Example:

- 1. Queuing in front of a counter
- 2. Traffic control at a turning point
- 3. Process synchronization in multi-user environment
- 4. Resource sharing in a computer centre.

Definition:

- Queue is an ordered collection of homogeneous data elements.
- ▶ It permits insertion of new element at one end.
- > Deletion of an element at the other end.
- > The **deletion** (**DEQUEUE**) of an element take place is called **front**.
- \geq The **insertion** (**ENQUEUE**) of a new element can take place is called **rear**.
- An element which enter first into the queue is the first element to delete from queue so it is called **First In First out (FIFO)**

<u>Representation</u> of Queue:

- There are two ways to represent a queue in memory: \geq
 - 1. Using an array
 - 2. Using linked list

1. Representation of queue using Array:

- A queue is first in, first out (FIFO) data structure.
- \geq Inserting at one end (the rear).

2

Deleting from the other (the front). 3





4

front = 0

Algorithm Enqueue (Item)

Steps:

- 1. If (REAR=N) then
 - 1. Print "Queue is full"
 - 2. Exit
- 2. Else
 - 1. If(REAR=0) and (FRONT=0) 1. FRONT=1
 - 2. Endif
 - 3. REAR=REAR+1
 - 4. Q[REAR]=ITEM
- 3. Endif

4. Stop

Algorithm DEQUEUE ()

Step:

- 1. If (Front=0) then
 - 1. Print "Queue is empty"
 - 2. Exit
- 2. Else
 - 1. ITEM=Q[FRONT]
 - 2. IF (FRONT=REAR)
 - 1. REAR=0
 - 2. FRONT=0
 - 3. ELSE
 - 1. FRONT=FRONT+1
 - 4. ENDIF
- 3. End if
- 4. Stop

2. Representation of queue using Linked list:

- > Queue is a structure containing two pointers:
 - 1. Front
 - 2. Rear
- > Front: point to the head of the node.
- Rear: point to the end of the list (last node).
- Enque operates upon the rear pointer.
- > Deque operates upon the front pointer.
- Empty queue is represented by NULL front & rear pointers.

Various Queue Structure:

- 1. Circular Queue
- 2. Priority Queue
- 3. Dequeue

Circular Queue:

- In a circular queue, all nodes are treated as circular. Last node is connected back to the first node.
- > Circular queue is also called as **Ring Buffer.**
- Circular queue contains a collection of data which allows insertion of data at the end of the queue and deletion of data at the beginning of the queue.



```
Operation on Circular Queue:
    1. Insertion
    2. Deletion
Insertion Algorithm
                                              Deletion Algorithm
                                              [Underflow]
[Reset pointer position]
If (R = =N)
                                              If (F = = 0)
{
                                              {
        R \leftarrow 1
                                                       "Queue is Empty"
}
                                              }
Else
                                              Else
{
                                              {
        R \leftarrow R+1
                                                         X \leftarrow Q[rear]
}
                                               }
[Overflow]
                                              [Is the Front Pointer]
If (F = R)
                                              If (F = R)
                                              {
{
        "Queue is Empty"
                                                       "Queue is Empty"
}
                                              }
Else
                                              [Reset the Front]
                                              If (F = = N)
Q[rear] \leftarrow X
                                              {
                                                       "Queue is Empty"
}
[Is pointer]
                                              }
If (F = = 0)
{
F←1
}
```

Priority Queues

- ▶ Insert & delete operation based on the priority.
- If the elements in the queue are same priority, then the element deletes which is inserting first into the queue.

Priority Queue



Types of priority Queue:

- 1. Ascending priority queue.
- 2. Descending priority queue.
- 1. Ascending priority queue:
 - Elements can be inserted in any order.
 - Elements deleted which is smallest element in the queue.

2. Descending priority queue:

Elements can be inserted in any order.

> Elements deleted which is largest element in the queue.

Operation of priority queue:

- 1. Insertion insert item into queue.
- 2. Deletion delete item from queue.
- 3. Display display item in the queue.

Dequeue:

 \succ It is used as a stack.

> In queue all operations take place at one end of the queue. Example:



> In enqueue, add an item to the back of the queue.

> In dequeue, delete item from front of the queue.

Example:



Applications of Queues

1. Simulation:

- Simulation is a modeling of a real life problem (or) it is the method of a real life situation in the form of computer program.
- The main objectives of the simulation to study the real life situation under the control of various parameters which affects the real problem, and is a reach interest of system analysts or operation research scientists.
- Any process or situation that is to be simulated is called a system.
- A system is a collection of interconnected objects which accepts zero or more inputs and produces at least one output.
 - A system is discrete if the input/output parameters are of discrete values.
 Ex: Ticket reservation
 - A system is stochastic is based on the randomness.
 Ex: Ticket counter.

2.CPU scheduling in Multiprogramming Environment:

- ▶ A Single CPU has to serve more than one program simultaneously.
- Multiprogramming environments the CPU are categorized into three groups:
- Interrupts to be serviced.
- Verify of devices and terminals are connected with the CPU and they may interrupt at any moment to get a service from it.
- Interactive users to be services.
- > These are mainly student's programs in various terminals under execution.
- Batch jobs to be services.

3. Round-Robin Algorithm:

- Round-Robin (RR) algorithm, is a scheduling algorithm, and is designed for time sharing systems.
- Suppose there are n processes P1, P2....Pn required to be served by the CPU.
- > Different processes require different execution time.
- > P1 comes first than P2 comes in general.
- > RR algorithm, first decides a small unit of time, called a time quantum/slice.
- A time quantum is generally from 10 to 100 milliseconds.
- > CPU starts with P1. P1 gets CPU for instant of time; afterwards CPU switches to P2 and so on.
- ➢ When CPU reaches the end of time quantum of Pn it returns to P1 and the same process will be repeated.
- Implementation of RR scheduling algorithm circular queue is the best choice, because the process when it completes its execution required to be deleted from the queue and it is not necessarily from the front of the queue rather from any position.

LINKED LISTS

What is linked list?

- ➢ Linked list are linear data structure.
- Each node in the linked list is connected with its previous node which is a pointer to the node.
- > The nodes in the linked list can be added and deleted from the list.
- \succ The node have two field,



Advantages:

- Need not allocate memory beforehand.
- Memory can allocated when necessary.
- Facilitate dynamic memory allocation.
- Insertion and deletion can be handled efficiently without fixing memory size.
- Over array it uses exactly as much memory needs. The size of an array is fixed when it is created.

Disadvantage:

- Traversal is sequential.
- Does not support random access.
- Increase overhead for storing pointers for linking the data items.

Types of Linked List

- > Following are the various types of linked list.
 - 1. Single Linked List Item navigation is forward only.
 - 2. Doubly Linked List Items can be navigated forward and backward.
 - 3. Circular Linked List Last item contains link of the first element as next and the first element has a link to the last element as previous.

Single Linked List

A single linked list each node contains only one link which points the subsequent node in the list.
 (i) Representation of a Linked List in Memory:

- There are 2 ways to represent a linked list in a memory.
 - 1. Static representation using array
 - 2. Dynamic representation free pool of storage.

Static representation:

- Static representation of a single linked list maintains two arrays:
- One array for data and other for links.
- Two parallel arrays of equal size are allocated which should be sufficient to store the entire linked list.
Dynamic Representation:

- > The efficient way of representing a linked list is using free pool of storage.
- > There is a memory bank, and a memory manager.
- During the creation of linked list, whenever a node is required the request is placed to the memory manager, memory manager will then search the memory bank for the block requested and if found grants a desired block to the caller.

Operations on a single linked list:

- 1. Insertion of a node in the before head node.
- 2. Deletion of a node in the before head node.
- 3. Insertion of a node in the middle of the list.
- 4. Deletion of a node in the middle of the list.
- 5. Insertion of a node after the last node.
- 6. Deletion of a node after the last node

1. Insertion of a node in the before head node: <u>Algorithm:</u>

New_node \rightarrow next = head; Head = next_node;



2. Insertion of a node in the middle of the list.

Algorithm:

While (p1 = Insert position) { P=p→next; } Store_next = p→next;

 $P \rightarrow next = next_node;$

new_node→next= store_next;



3. Insertion of a node after the last node. <u>Algorithm:</u>

While (p1 = next! = null) $\begin{cases}
P = p \rightarrow next; \\
P \rightarrow next = next_node; \\
new_node \rightarrow next = null; \\
head
 10 \rightarrow 20 \rightarrow 30 \qquad 40 \\
newNod$



```
{
node *p,*q;
q=head;
p=head;
p=head \rightarrow next;
if (q\rightarrow data = ==d)
{
head = p;
delete (q);
}
else
{
While (p\rightarrow data!=d)
{
P=p\rightarrownext;
Q=q\rightarrownext;
}
}
```

5. Deletion of a node in the middle and last of the list.

Algorithm

```
If (p \rightarrow next = = null)
{
q \rightarrow next = null;
delete (p);
}
Else
{
q \rightarrow next = p \rightarrow next;
delete (p);
}}
```

2. Doubly linked list

- Each node contains data and two links, one link pointing to the previous node and one link pointing to the next node.
- Suppose we are in middle, again traverse from starting node. This is drawback of singly linked list.
- ▶ In Doubly linked list can be traversed forward and backward.
- Each node there are 2 links are represented
- 1. address of the previous item
- 2. represent next item

3. Circular Linked List

- Circular Linked List is a variation of Linked list in which the first element points to the last element and the last element points to the first element.
- > Both Singly Linked List and Doubly Linked List can be made into a circular linked list.

Singly Linked List as Circular

➤ In singly linked list, the next pointer of the last node points to the first node.



Doubly Linked List as Circular

➤ In doubly linked list, the next pointer of the last node points to the first node and the previous pointer of the first node points to the last node making the circular in both directions.



> As per the above illustration, following are the important points to be considered.

- The last link's next points to the first link of the list in both cases of singly as well as doubly linked list.
- > The first link's previous points to the last of the list in case of doubly linked list.

Basic Operations

- > Following are the important operations supported by a circular list.
 - 1. Insert Inserts an element at the start of the list.
 - 2. Delete Deletes an element from the start of the list.
 - 3. Display Displays the list.

Insertion Operation

Following code demonstrates the insertion operation in a circular linked list based on single linked list.

Example

Following code demonstrates the deletion operation in a circular linked list based on single linked list. //delete first item

```
struct node * deleteFirst() {
    //save reference to first link
    struct node *tempLink = head;
```

```
if(head->next == head) {
    head = NULL;
    return tempLink;
```

```
}
```

}

//mark next to first link as first
head = head->next;

//return the deleted link
return tempLink;

Display List Operation

Following code demonstrates the display list operation in a circular linked list.
//display the list
void printList() {
 struct node *ptr = head;
 printf("\n[");
 //start from the beginning
 if(head != NULL) {

```
while(ptr->next != ptr) {
    printf("(%d,%d) ",ptr->key,ptr->data);
    ptr = ptr->next;
    }
}
```

printf("]");

}

Application of Linked Lists

1. Sparse matrix manipulation:



- > The fields I and j store the row & column for a matrix element.
- > Data field stores the matrix element at the i^{th} row and the j^{th} column. ie) a_{ij} .
- The ROWLINK points to the next node in the same row and COLLINK points the next node in the same column.
- All the nodes particularly in a row (column) are circular linked with each other each row (column) contains a header node.
- A sparse matrix of order m*n, we have to maintain m headers for all rows and n headers for all columns, plus one extra node use of which can be evident.

2. Polynomial

- > A polynomial is a mathematical expression consisting of a sum of terms.
- > Each term including a variable or variables raised to a power and multiplied by a coefficient.
- An essential characteristic of the polynomial is that each term in the polynomial expression consists of two parts:
 - 1. one is the coefficient
 - 2. other is the exponent

Example:

 $10x^2 + 26x$

10 & 26 \rightarrow Coefficients

2 & 1 \rightarrow Exponential value.

Points to keep in Mind while working with Polynomials:

- > The sign of each coefficient and exponent is stored within the coefficient and the exponent itself
- > Additional terms having equal exponent is possible one.
- The storage allocation for each term in the polynomial must be done in ascending and descending order of their exponent



Representation of polynomial using linked list:

- > A polynomial can be thought of as an ordered list of non zero terms. Each non zero term is a twotuple which holds two pieces of information:
 - 1. The exponent part
 - 2. The coefficient part

UNIT-III Question Bank

One word question and answers:	
1. A linear list of elements in which deletion can be done from one end (front) and	l insertion can take
place only at the other end (rear) is known as a ?	
a) Queue b) Stack c) Tree d) Linked list	Answer: a
2. The data structure required for Breadth First Traversal on a graph is?	Angewone
a) Stack b) Array c) Queue d) Tree	Answer: c
5. A queue follows	a) Ordered array
d) Linear tree Answer: a	c) Ordered array
4. Circular Queue is also known as	
a) Ring Buffer b) Square Buffer c) Rectangle Buffer d) Curve Buff	er Answer: a
5. If the elements "A", "B", "C" and "D" are placed in a queue and are deleted or	e at a time, in what
order will they be removed?	- ··· · · · · · · · · · · · · · · · · ·
a) ABCD b) DCBA c) DCAB d) ABDC	Answer: a
6. A data structure in which elements can be inserted or deleted at/from both the e	nds but not in the
middle is?	
a) Queue b) Circular queue c) Dequeue d) Priority queue	Answer: c
7. A normal queue, if implemented using an array of size MAX_SIZE, gets full w	hen
a) Rear = MAX_SIZE -1 b) Front = (rear $+1$)mod MAX_SIZE a) Front = (rear $+1$) mod MAX_SIZE	A
c) Front = rear + 1 d) Rear = front 8. Queues serve major role in	Answer: a
a) Simulation of recursion b) Simulation of arbitrary linked list	
c) Simulation of limited resource allocation d) Simulation of heap sort	Answer: c
9. Which of the following is not the type of queue?	
a) Ordinary queue b) Single ended queue c) Circular queue d) Pri-	ority queue
Answer: b	
10. A linear collection of data elements where the linear node is given by means o	f pointer is called?
a) Linked list b) Node list c) Primitive list d) Unordered list	Answer: a
11. Consider an implementation of unsorted singly linked list. Suppose it has its re	epresentation with a
Read pointer only.	d in $O(1)$ time?
i) Insertion at the front of the linked list ii) Insertion at the end of the li	nked list
iii) Deletion of the front node of the linked list iv) Deletion of the last node of	the linked list
a) I and II b) I and III c) I, II and III d) I, II and IV	Answer: b
12. In linked list each node contain minimum of two fields. One field is data field	to store the data
second field is?	
a) Pointer to character b) Pointer to integer c) Pointer to node d) No	deAnswer: c
13. The concatenation of two list can performed in $O(1)$ time. Which of the follow	ring variation of
linked list can be used?	
a) Singly linked list b) Doubly linked list c) Circular doubly linked list d) Array implementation of list Answer: c	
14. What kind of linked list is best to answer question like "What is the item at pos	sition n?"
a) Singly linked list b) Doubly linked list c) Circular linked list	
d) Array implementation of linked list Answer: d	
15. Linked lists are not suitable to for the implementation of?	
a) Insertion sort b) Radix sort c) Polynomial manipulation d) Bir	nary search
Answer: d	-
16. Linked list is considered as an example of type of memory alloc	ation.
a) Dynamic b) Static c) Compile time d) Heap	Answer: a
17. In Linked List implementation, a node carries information regarding	
a) Data b) Link c) Data and Link d) Node	Answer: b
18. Linked list data structure offers considerable saving in	
a) Computational Time b) Space Utilization	Answork
c) space offization and computational time (d) speed offization	Answer: C

19. Which of the following points is/are not true about Linked List data s with array?	tructure when it is compared
a) Arrays have better cache locality that can make them better in terms	s of performance
c) Random access is not allowed in a typical implementation of Linke	d L ists
d) Access of elements in linked list takes less time than compared to a	arravs Answer: d
20. Which of the following sorting algorithms can be used to sort a random	m linked list with minimum
time complexity?	
a) Insertion Sort b) Quick Sort c) Heap Sort d) Merge Sort	t Answer: d
21. Which of the following is false about a doubly linked list?	
a) We can navigate in both the directions	
b) It requires more space than a singly linked list	
d) Implementing a doubly linked list is easier than singly linked list	Answer: d
22. How do you calculate the pointer difference in a memory efficient do	ible linked list?
a) head xor tail b) pointer to previous node xor pointer to next	node
c) pointer to previous node – pointer to next node	
d) pointer to next node – pointer to previous node	Answer: b
23. What differentiates a circular linked list from a normal linked list?	
a) You cannot have the 'next' pointer point to null in a circular linked	list
b) It is faster to traverse the circular linked list	1. 1. 11. /
c) You may or may not have the 'next' pointer point to null in a circul	ar linked list
a) Head node is known in circular linked list 24. Which of the following application makes use of a circular linked list	Answer: c
a) Undo operation in a text editor b) Recursive function calls	
c) Allocating CPU to resources d) Implement Hash Tables	Answer: c
25. Which of the following properties is associated with a queue?	
a) First In Last Out b) First In First Out c) Last In First Out	d) Last In Last Out
Answer: b	
26. What is the term for inserting into a full queue known as?	
a) overflow b) underflow c) null pointer exception d) program v	won't be compiled Answer: a
27. What is the need for a circular queue?	amonts based on priority
d) implement LIFO principle in queues Answer: a	ements based on priority
28. In linked list implementation of queue, if only front pointer is maintain	ned, which of the following
operation take worst case linear time?	
a) Insertion b) Deletion c) To empty a queue d) Both Insertion and '	To empty a queue Answer: d.
29. In linked list implementation of a queue, where does a new element be	e inserted?
a) At the head of link list b) At the centre position in the link lis	t .
c) At the tail of the link list d) At any position in the linked list	Answer: c
Explanation: Since queue follows FIFO so new element inserted at las	St.
so. In mixed list implementation of a queue, none and real pointers are us nointers will change during an insertion into a NONEMPTY queue?	acked. Which of these
a) Only front pointer b) Only rear pointer c) Both front and rear	pointer
d) No pointer will be changed	Answer: b
Explanation: Since queue follows FIFO so new element inserted at las	st.
31. In linked list implementation of a queue, front and rear pointers are tra	acked. Which of these
pointers will change during an insertion into EMPTY queue?	
a) Only front pointer b) Only rear pointer c) Both front and rear	pointer
d) No pointer will be changed Answer: c	1
32. In case of insertion into a linked queue, a node borrowed from the	list is inserted in the queue.
a) AVAIL U) FROM C) REAR (1) MULL 33 In linked list implementation of a queue from where is the item delete	Answer: a
a) At the head of link list b) At the centre position in the link lis	t
c) At the tail of the link list d) Node before the tail	Answer: a

34. In linked list implementation of a queue, the important condition fora) FRONT is nullb) REAR is nullc) LINK is empty	a queue to be empty is? d) FRONT==REAR-
35. The essential condition which is checked before insertion in a linkeda) Underflow b) Overflow c) Front value d) Rear value	queue is? Answer: b
36. The essential condition which is checked before deletion in a linked a) Underflowb) Overflowc) Front valued) Rear value	queue is? e Answer: a
37. Which of the following is true about linked list implementation of qua) In push operation, if new nodes are inserted at the beginning of lin nodes must be removed from endb) In push operation, if new nodes are inserted at the beginning, then	eue? ked list, then in pop operation, in pop operation, nodes must
be removed from the beginningc) In push operation, if new nodes are inserted at the end, then in pop removed from endd) In push operation, if new nodes are inserted at the end, then in pop	o operation, nodes must be
removed from beginning	Answer: a
38. With what data structure can a priority queue be implemented?	
a) Array b) List c) Heap d) Tree	Answer: d
39. Which of the following is not an application of priority queue?	
a) Huffman codes b) Interrupt handling in operating system	
c) Undo operation in text editors d) Bayesian spam filter	Answer: c
40. What is a dequeue?	1
a) A queue with insert/delete defined for both front and rear ends of t	the queue
b) A queue implemented with both singly and doubly linked lists	
d) A queue millemented with both singly and doubly miked lists	A nowowe o
41 What are the applications of dequeue?	Allswei.a
a) A-Steal job scheduling algorithm b) Can be used as both stack	and queue
c) To find the maximum of all sub arrays of size k d) To avoid	collision in hash tables
Answer: d	
5 Marks	

- 1. Explain various representations of Queues.
- 2. Discuss in detail about circular Queue and its implementation.
- 3. Discuss in detail about circular De- Queue.
- 4. Explain the applications of queues.
- 5. Explain priority queue and its operations

10 marks

- 1. What is Queue? Why it is known as FIFO? Write an algorithm to insert and delete an element from a simple Queue.
- 2. What are Circular Queue and Priority Queue? Write an algorithm to insert and delete an element from a Circular Queue.
- 3. What do you mean by Link list? Write an algorithm to insert and delete a node in Singly Linked List.
- 4. What is Doubly Linked List? Write an algorithm to insert and delete a node in Doubly Linked List.
- 5. What is Circular Linked List? State the advantages and disadvantages of Circular Link List Over Doubly Linked List and Singly Linked List. Also write advantages of Linked List over an Array.

_____END_____

UNIT-IV

TREES

Introduction about Trees:

A tree is a very flexible and powerful data structure that can be used for a wide variety of applications.

> Each tree node contains a name for data and one or more pointers to the other tree nodes.



Basic Terminology:

- ✓ **Node**: Each element presents in a binary tree is called a node of that tree.
- ✓ **Parent:** Parent of a node is the immediate predecessor of a node
- ✓ **Root:** The element represent the base node of the tree is called the root of the tree.
- ✓ Child: If the immediate predecessor of a node is the parent of the node then all immediate successors of a node are known as child.
- ✓ **Link:** This is a pointer to a node in a tree.
- ✓ Left and Right sub trees: Apart from the root, the other two sub sets of binary trees are binary trees. They are called the left and right sub trees of the original tree.
- \checkmark Leaf node: A node that does not have any sons.
- ✓ **Degree:** The number of sub trees of a node.
- ✓ **Interior or non-interior nodes**: Nodes that have degree > 0.
- ✓ **Parent and child:** The roots of the sub trees of a node are called the children of that node.
- ✓ **Siblings:** Children's of the same parent are said to be siblings.
- ✓ Ancestors: The ancestors of anode are all the nodes along the path from the root of that node.
- ✓ Level: The level of anode is defined by initially letting the root be at level1. If a node is at level p, then its children are at level P+1.
- ✓ **Height or depth**: The height of a tree is defined to be the maximum level of any node in the tree.
- ✓ **Forest:** A forest is a set of $n \ge 0$ disjoint trees.
- ✓ Path length of a node: The number of edges needed to reach specified node form the root is called its path length.
- ✓ **Internal path**: The sum of path length of all the nodes in the tree.

Simple Binary tree



- > A Binary Search Tree (BST) is a tree in which all the nodes follow the below-mentioned properties
- 1. The left sub-tree of a node has a key less than or equal to its parent node's key.
- 2. The right sub-tree of a node has a key greater than to its parent node's key.

Definition and Concepts

Binary trees:

- A binary tree consists of a finite set of elements that can be partitioned into three distinct subsets called the root, the left and right sub tree.
- \blacktriangleright If there are no elements in the binary tree it is called an empty binary tree.

Full Binary Tree:

- > All nodes have two children.
- ➢ Each sub-tree has same length of path.



Complete binary tree:

- All nodes have two children.
- ► Each sub-tree has different length of path.



REPRESENTATION OF A BINARY TREE

Array representation

- > An array is used to store the nodes of the binary tree.
- ▶ Nodes stored in the array area access sequentially.
- > Root is at index 0, and then left child and right child are stored.



Declare array of size 2 ³⁺¹ -1 = 15 Char a[15]



Linked representation of binary trees:

- > In linked list every element is represented as nodes.
- ➤ A node consists of three fields such as,
 - 1. Left child
 - 2. Information node
 - 3. Right child



- > The left child point to the left child of parent node.
- > The right child point to the right child of parent node.
- > The information holds the information of every node.

OPERATIONS ON A BINARY TREE

- ✓ **Insertion**: To include a node into an existing binary tree.
- ✓ **Deletion:** To delete a node from a non-empty binary tree.
- ✓ **Traversal:** To visit all the nodes in a binary tree.
- ✓ **Merge:** To merge two binary trees into a larger one.

Insertion Algorithm		Deletion Algorithm	
Algorithm for inserting a node:	The node containing the data has no children	The node containing the data has one children	The node containing the data has two children
Struct node* curr; Curr=root; While(curr) { Parent=cur; If(t→data > curr→data) { Curr=curr→right; } Else { Curr=curr→left; } If(t→data> parent→data) { Parent→right=t; } Else { Parent→left=t; }	If(curr==parent→left) { Parent→left=null; } Else { Parent→right=null; } Free(curr); }	If(curr→left!=null) { If(curr==parent→left) { Parent→left=cur→left; } Curr→left=null; Free(curr); }	If(curr \rightarrow left!=null && cur \rightarrow right!=null) { Int t; T=curr \rightarrow right; If(t \rightarrow right!=null && t \rightarrow left==null) { Curr \rightarrow data=t \rightarrow data; Curr \rightarrow right=t \rightarrow right; T \rightarrow right=null; Free(t); }

TRAVERSAL OF A BINARY TREE

- > Traversal is a process to visit all the nodes of a tree and may print their values.
- > That is, we cannot randomly access a node in a tree.
- > There are three ways which we use to traverse a tree
 - 1. In-order Traversal
 - 2. Pre-order Traversal
 - 3. Post-order Traversal

In-order Traversal

- > In this traversal method, the left subtree is visited first, then the root and later the right sub-tree.
- ▶ We should always remember that every node may represent a subtree itself.
- If a binary tree is traversed in-order, the output will produce sorted key values in an ascending order. Root



Left Subtree Right Subtree

- $D \to B \to E \to A \to F \to C \to G$
 - ▶ We start from A, and following in-order traversal, we move to its left subtree B.
 - ▶ B is also traversed in-order. The process goes on until all the nodes are visited.
 - > The output of inorder traversal of this tree will be –

Algorithm

Until all nodes are traversed -

Step 1 – Recursively traverse left subtree.

Step 2 – Visit root node.

Step 3 – Recursively traverse right subtree.

Pre-order Traversal

> In this the root node is visited first, then the left subtree and finally the right subtree.



Right Subtree $A \to B \to D \to E \to C \to F \to G$

- We start from A, and following pre-order traversal, we first visit A itself and then move to its left subtree B.
- ▶ B is also traversed pre-order. The process goes on until all the nodes are visited.
- > The output of pre-order traversal of this tree will be -

Algorithm

Until all nodes are traversed -

Step 1 – Visit root node.

Step 2 – Recursively traverse left subtree.

Step 3 – Recursively traverse right subtree.

Post-order Traversal

In this traversal method, the root node is visited last, hence the name. First we traverse the left subtree, then the right subtree and finally the root node.



$\begin{array}{cc} \text{Right Subtree} & D \to E \to B \to F \to G \to C \to A \end{array}$

- > We start from A, and following Post-order traversal, we first visit the left subtree B.
- ➢ B is also traversed post-order.
- > The process goes on until all the nodes are visited.
- > The output of post-order traversal of this tree will be -

Algorithm

- Until all nodes are traversed –
- Step 1 Recursively traverse left subtree.
- Step 2 Recursively traverse right subtree.
- Step 3 Visit root node.

TYPES OF BINARY TREES

There are several types of binary trees

- 1. Expression tree
- 2. Binary search tree
- 3. Heap tree
- 4. Threaded binary tree
- 5. Huffman binary tree
- 6. Height balanced tree (AVL tree)
- 7. Decision tree

1. Expression tree:

- > An expression tree is a binary tree which stores an arithmetic expression.
- > The leaves of an expression tree are operand, such as constants or variable names and all internal nodes are the operators.
- Expression tree is always a binary tree because an arithmetic expression contains either binary operator or unary operator.

a * (b + c) + d



Operations on the expression tree:

- > There are two operations are possible on any expression tress:
 - 1. Traversing
 - 2. Evaluating
- > Traversal operations are same as binary tree such as inorder, preorder and postorder.
- > Evaluating of the expression is to evaluate the expression for which the tree is found.

3. HEAP TREES

Heap is a binary tree such that the value at a node N is > or = the value at each of the children of node N.

Min-Heap:

▶ Where the value of the root node is less than or equal to either of its children.



Max-Heap:

 \blacktriangleright Where the value of the root node is greater than or equal to either of its children.



Representation of a heap tree:

> A heap tree can be represented using linked structure.

Operations on heap tree:

- 1. Insert into a heap tree
- 2. Deletion of a node
- 3. Merging two heap trees

<u>1. Insert into a heap tree</u>

- > This operation is used to insert a node into an existing heap tree satisfy the properties if heap tree.
 - Step 1 Create a new node at the end of heap.
 - Step 2 Assign new value to the node.
 - Step 3 Compare the value of this child node with its parent.
 - Step 4 If value of parent is less than child, then swap them.
 - Step 5 Repeat step 3 & 4 until Heap property holds.

2. Deletion of a node from a heap tree:

- Any node can be deleted from a heap tree. Deleting the root node has some special importance.
 - Step 1 Remove root node.
 - Step 2 Move the last element of last level to root.
 - Step 3 Compare the value of this child node with its parent.
 - Step 4 If value of parent is less than child, then swap them.
 - Step 5 Repeat step 3 & 4 until Heap property holds.

3. Merging two heap tree

The two heap trees H1 and H2. Merging the tree H2 with H1 means to include all the nodes from H2 to H1. H2 may be min heap or max heap and the resultant tree will be min heap if H1 is min heap else it will be max heap.

This operation consists of two steps:

- 1. Delete the root node say x from H2.
- 2. Insert the node x into H1 satisfying the property of H1.

RED-BLACK TREE

A red-black tree is a binary search tree which has the following *red-black properties*:

1. Every node is either red or black.

- 2. Every leaf (NULL) is black.
- 3. If a node is red, then both its children are black.
- 4. Every simple path from a node to a descendant leaf contains the same number of black nodes.



GRAPHS

Introduction:

- ➢ Graph is another non-linear data structure.
- > It is hierarchical relationship between parent and children's.

Application:

- Airlines
- Source-destination network
- Konigsberg's bridges.
- Flowchart of a program

Graph Terminology:

Graph:

• A graph consist of two sets

- (i) A set V called set of all vertices (or node)
 - (ii) A set E called set of all edges (or arcs)m
 - Set of vertices = $\{1,2,3\}$
 - Set of edges= $\{ (1,2), (1,3) \}$

Digraph:

- > A digraph is also called a directed graph. If a graph G, such that $G = \langle V, E \rangle$, where V is the set of all vertices and E is the set of ordered pair of elements from V.
- \blacktriangleright Here G2 is a Digraph where

$$V = \{v1, v2, v3, v4\}$$

$$E = \{(v1, v2), (v1, v3), (v2, v3), (v3, v4), (v4, v1)\}$$

Weighted graph:

- > A graph is termed as weighted graph if all the edges in it are labeled with some weight.
- Ex: G3 and G4 are two weighted graphs.

Adjacent vertices:

- A vertex v_i is adjacent to another vertex say v_j if there is an edge from v_i to v_j .
- \blacktriangleright Ex: Graph G11, v2 is adjacent to v3 and v4.

Self loop:

- If there is an edge whose starting and end vertices are same, that is (vi,vj) is an edge then it is called a self loop.
- ► Ex: GraphG5

Parallel edges:

- ➢ If there are more than one edges between the same pair of vertices, then they are known as the parallel edge.
- Ex: Graph G5.

Multi graph:

- > A graph which has either self loop or parallel edges or both is called multi graph.
- \succ Ex: Graph G5.

Simple graph (digraph):

> A graph if it does not have any self loop or parallel edges is called a simple graph.

► Ex: graph G5.

Complete graph:

- A graph G is said to be complete if each vertex vi adjacent to every other vertex vj in G
- ► Ex: Grapg G6 and G9.

Acyclic graph:

- If there is a path containing one or more edges which starts from a vertex vi and terminates into the same vertex then the path is known as a cycle.
- \blacktriangleright Ex: graph G4 and G7.

Isolated vertex:

- > A vertex is isolated if there is no edge connected from any other vertex to the vertex.
- ➢ Ex: Graph G8.

Degree of vertex:

- The number of edges connected with vertex v_i called the degree of vertex v_i and is denoted by degree (v_i).
- > In digraph there are two degrees: indegree and ourdegree.
- > **Indegree** of v_i denoted as indegree (v_i) = number of edges incident into v_i .
- > **Outdegree**(vi) = number of edges emanating from vi.
- Ex: In graph G4indegree(v_1)=2 outdegree(v_1)=1
- indegree(v_2)=2 outdegree(v_1)=0

Pendent vertex:

- A vertex v_i is pendent if its indegree(v_i)=1 and outdegree (v_i)=0
- \succ Ex: G8 is a pendent vertex.

Connected graph:

- > In a graph G two vertices v_I and v_j are said to be connected if there is a path in G from v_i to v_j .
- \succ A graph is said to be connected if for every pair of distinct vertices v_i, v_j in G there is a path.
- Ex: Graph G1, G3 and G6.

REPRESENTATION OF GRAPHS

- ➢ A graph can be represented in many ways
 - 1. Set representation
 - 2. Linked representation
 - 3. Sequential (matrix) representation

(i) Set representation:

This is one of the straightforward methods of representing a graph. In this method two sets are maintained (i) V is the set of vertices

(ii) E is the set of edges.

Graph G1

V(G1)= { v1,v2,v3,v4,v5,v6,v7}

 $E(G1)=\{ (v1,v2), (v1,v3), (v2,v4), (v2,v5), (v3,v6), (v3,v7) \}$

Graph G2

 $V(G2) = \{ v1, v2, v3, v4, v5, v6, v7 \}$ E(G2) = { (v1, v2), (v1, v3), (v2, v4), (v2, v5), (v3, v4), (v3, v6), (v4, v7), (v5, v7), (v6, v7) }

Graph G3

 $V(G3) = \{ A,B,C,D,E \}$ E(G3)= { (A,B), (A,C), (C,B), (C,A),(D,A),(D,B),(D,C),(D,E),(E,B) } Graph G4 V(G4)= { A,B,C,D } E(G4)= { (3,A,C), (5,B,A), (1,B,C), (7,B,D),(2,C,A),(4,C,D),(6,D,B),(8,D,C) }

(ii) Linked representation:

- ▶ Linked representation is another space-saving way of graph representation.
- Node structure is,



- Linked representation of graphs, the number of lists depends on the number of vertices in the graph.
- The header node in each list maintains a list of all adjacent vertices of anode for which header node is meant.

iii. Matrix Representation

The adjacency matrix is represents in 2D array of size n*n matrix in which n is the number of vertices.

Ex: A[i][j]=1 means that the adjacency matrix has one edge.

A[i][j]=0 means that the adjacency matrix has no edges.



Adjacency matrix for undirected graph:

- > The adjacency matrix for an undirected graph is symmetric.
- > The adjacency matrix for a directed graph need not be symmetric.
- > The space needed to represent a graph using its adjacency matrix is n^2 locations.

OPERATIONS ON GRAPHS

Insertion

- > To insert a vertex and hence establishing connectivity with other vertices in the existing graph
- \blacktriangleright To insert an edge between vertices in the graph.

Deletion

- \succ To delete a vertex from the graph.
- \blacktriangleright To delete an edge from the graph.

Merging

To merge two graph G1 and G2 into a single graph.

<u>Traversal</u>

> To visit all the vertices in the graph.

Operations on Linked List Representation of Graphs:

- \succ In this representation using two representations.
- (i) An array of vertices having two fields: LABEL label for the vertices, LINK-the pointer to the linked list.
- (ii) A linked list to maintain the list of all adjacent vertices for any vertex vi for which it is meant.
- (iii) A node structure has two fields other than the filed LINK.
- (iv) The first field WEIGHT is to store the weight of the edge and the second field LABLE to store the vertex's label

Insertion

- > Insertion procedure differs for undirected graph and directed graph.
- To insert of a vertex into an undirected graph, if V_x is inserted and V_i be its adjacent vertex V_i has to be incorporated in the adjacency list of V_x as well as has to be incorporated in the adjacency list of V_i.
- > If it's a digraph and if there is a path from V_x to V_i we add a node for V_i into the adjacency list of V_x , if there is an edge from V_i to V_x add a node for V_x in the adjacency list of V_i .

1) Algorithm INSERT_VERTEX_LL_UG(V_x, X)

Vx is the new vertex that has to be inserted into a graph. $\tilde{\boldsymbol{\omega}}$

Steps:

- 1. N=N+1, V_x =N
- 2. For i=1 to 1 do
 - 1. Let j=X[i]
 - 2. If $(j \ge N)$ then
 - 1. Print "No vertex labeled X[i] exist; edge from V_x into the list of vertices."
 - 3. Else
- 1. INSERT_SL-END(UGptr[N],x[i])
- 2. INSERT_SL-END(UGptr[j],Vx)
- 4. Endif
- 3. Endfor
- 4. Stop

2) Algorithm INSERT_VERTEX_LL_DG(V_x, X,Y) Vx is the new vertex that has to be inserted into a graph. Steps:

- 1. N=N+1, $V_x=N$
- 2. For i=1 to m do
 - 1. Let j=X[i]
 - 2. If $(j \ge N)$ then
 - 1. Print "No vertex labeled X[i] exist; edge from V_x to X[i] is not established"
 - 3. Else
 - 1. INSERT_SL-END (DGptr[N],x[i])
 - 4. Endif
- 3. Endfor
- 4. For i=1 to n do
 - 1. Let j=Y[i]
 - 2. If $(j \ge N)$ then
 - 1. Print "No vertex labeled Y[i] exist; edge from V_x to X[i] is not established"
 - 3. Else
 - 1. INSERT_SL-END (DGptr[j],Vx)
 - 4. Endif
- 5. Endfor
- 6. stop

3) Insert the edge between two vertices in Undirected graph: Algorithm: INSERT EDGE LL UG(Vi,Vj)

Insert the edge to be inserted between vertices Vi and Vj.

Steps:

- 1. Let N=number of vertices in the graph
- 2. If (Vi>N) or (Vj>N) then
 - 1. Print" Edge is not possible between Vi and Vj"
- 3. Else
 - 1. INSERT_SL_END (UGptr[Vi],Vj"
 - 2. INSERT_SL_END (UGptr[Vj],Vi"
- 4. Endif
- 5. Stop

4)Insert the edge between two vertices in directed graph: Algorithm: INSERT_EDGE_DG (Vi,Vj)

Insert the edge to be inserted between vertices Vi and Vj.

Steps:

- 1. Let N=number of vertices in the graph
- 2. If(Vi>N) or (Vj>N) then
 - 1. Print" Edge is not possible between Vi and Vj"
- 3. Else
 - 1. INSERT_SL_END (UGptr[Vi],Vj")
- 4. Endif
- 5. Stop

<u>Deletion:</u> 1) Delete the vertex: Algorithm Delete_Vertex_LL_UG (Vx) Step:

- 1. If (N=0) then
 - 1. Print" Graph is empty : No deletion"
 - 2. Exit
- 2. Endif
- 3. ptr=UGptr[Vx] . LINK
- 4. While($ptr \neq NULL$) do
 - 1. j=ptr.LABEL
 - 2. DELETE_SL_ANY(UGptr[j],Vx)
 - 3. DELETE_SL_ANY(UGptr[Vx], j)
 - 4. ptr=UGptr[Vx].LINK
- 5. Endwhile
- 6. UGptr[Vx].LABEL=NULL
- 7. UGptr[Vx].LINK=NULL
- 8. RETURN_NODE(ptr)
- 9. N=N-1
- 10. Stop

2) To delete the edge between vertices Vi and Vj Algorithm: Delete_Edge_LL_UG(Vi,Vj)

- 1. let N=number of vertices in the graph
- 2. if(Vi>N) or (Vj>N) then
 - 1. Print "Vertex does not exist: Error in edge removal"
- 3. Else
 - 1. DELETE_SL_ANY(UGptr[Vi],Vj)
 - 2. DELETE_SL_ANY(UGptr[Vj],Vi)
- 4. Endif
- 5. Stop

GRAPH TRAVESAL

In the traversal of a binary tree there are two ways as follows.

- > Depth First search
- Breadth first search

Depth First Search:

Depth First Search (DFS) algorithm traverses a graph in a depthward motion and uses a stack to remember to get the next vertex to start a search, when a dead end occurs in any iteration.



- As in the example given above, DFS algorithm traverses from S to A to D to G to E to B first, then to F and lastly to C.
- ➢ It employs the following rules.
 - 1. Rule 1 Visit the adjacent unvisited vertex.
 - 2. Mark it as visited.
 - 3. Display it.
 - 4. Push it in a stack.
 - 5. Rule 2 -If no adjacent vertex is found, pop up a vertex from the stack.
 - 6. It will pop up all the vertices from the stack, which do not have adjacent vertices.
 - 7. Rule 3 Repeat Rule 1 and Rule 2 until the stack is empty.

Breadth First Search:

Breadth First Search (BFS) algorithm traverses a graph in a breadthward motion and uses a queue to remember to get the next vertex to start a search, when a dead end occurs in any iteration.



- As in the example given above, BFS algorithm traverses from A to B to E to F first then to C and G lastly to D. It employs the following rules.
 - 1. Rule 1 Visit the adjacent unvisited vertex.
 - 2. Mark it as visited.
 - 3. Display it.
 - 4. Insert it in a queue.
 - 5. Rule 2 If no adjacent vertex is found, remove the first vertex from the queue.

6. Rule 3 – Repeat Rule 1 and Rule 2 until the queue is empty.

APPLICATION OF GRAPH STRUCTURES

- ➢ Graph is an important data structure whose extensive applications are known in almost all application areas.
- Conversion of a particular problem into this general graph theoretic problem will rest on the reader.
 - 1. Shortest path problem
 - 2. Topological sorting of a graph
 - 3. Spanning trees

SHORTEST PATH PROBLEM

- The shortest path problem is about finding a path between 2 vertices in a graph such that the total sum of the edges weights is minimum.
- > To find shortest problem, we have three algorithm,
 - 1. Floyd & Warshall's Algorithms
 - 2. Dijkstra's Algorithm

Warshall's Algorithms:

This is a classical algorithm by which we can determine whether there is a path from any vertex Vi to another vertex Vj either directly or through one or more intermediate vertices.

Steps:

11. For i=0 to N do

- 1. For j=1 to N do
 - 1. P[i][j]= Gptr[i][j]
- 2. Endfor
- 12. End for
- 13. For k=1 to N do
 - 1. For i=1 to N do
 - 1. For j=1 to N do

```
1. P[i][j] = P[i][j] v (P[i][k] ^ P[k][j])
```

2. Endfor

- 2. Endfor
- 14. End for
- 15. Return(p)
- 16. Stop

Floyd's Algorithm:

> The basic structure of the Floyd's algorithm is same as Warshall's algorithm.

Steps:

1. For i=1 to N do 1. For j=1 to N do 1. If (Gptr[i][i] = 0) then 1. $Q[i][j] = \infty$ 2. PATHS[i][j]=NULL 2. Else 1. Q[i][j]=Gptr[i][j] 2. P=COMBINE (i,j) 3. PATHS[i][j]=P 3. Endif 2. Endfor 2. Endfor 3. For k=1 to N do 1. For i=1 to N do 1. For j=1 to N do 1. Q[i][j] = MIN(Q[i][j], Q[i][k] + Q[k][j])

2. If (Q[i][k]+Q[k][j]<Q[i][j]) then 1. p1= PATHS[i][k] 2. p2= PATHS[k][j] 3. PATHS[i][j]=COMBINE(p1,p2)

3. Endif

2. Endfor

2. Endfor

4. End for

5. Return (Q, PATHS)

6. Stop

Dijkstra's Algorithm:

Dijkstra's algorithm solves the single-source shortest-paths problem on a directed weighted graph G = (V, E), where all the edges are non-negative.

Example

- Let us consider vertex 1 and 9 as the start and destination vertex respectively.
- > Initially, all the vertices except the start vertex are marked by ∞ and the start vertex is marked by 0.

Vertex	Initial	Step1 V1	Step2 V3	Step3 V2	Step4 V4	Step5 V5	Step6 V7	Step7 V8	Step8 V6
1	0	0	0	0	0	0	0	0	0
2	x	5	4	4	4	4	4	4	4
3	∞	2	2	2	2	2	2	2	2
4	∞	∞	∞	7	7	7	7	7	7
5	x	∞	x	11	9	9	9	9	9
6	x	∞	x	∞	x	17	17	16	16
7	∞	∞	11	11	11	11	11	11	11
8	∞	∞	∞	∞	∞	16	13	13	13
9	x	x	∞	x	x	∞	x	∞	20

→ Hence, the minimum distance of vertex 9 from vertex 1 is 20. And the path is $1 \rightarrow 3 \rightarrow 7 \rightarrow 8 \rightarrow 6 \rightarrow 9$



Topological Sorting:

- Topological sorting is an ordering of vertices of a graph, such that if there is a path from u to v in the graph then u appears before v in the ordering.
- A topological ordering is not possible if the graph has a cycle, since for two vertices u and v on the cycle, u precedes v and v precedes u.

A simple algorithm to find a topological ordering is to find out any vertex with in degree zero, that is vertex without any predecessor.



Algorithm:

Begin

Initially mark all nodes as unvisited For all nodes v of the graph, do If v is not visited, then TopoSort (i, visited, stack) Done Pop and print all elements from the stack End.

MINIMUM SPANNING TREE

- ➤ A spanning tree is a subset of Graph G, which has all the vertices covered with minimum possible number of edges.
- > Hence, a spanning tree does not have cycles and it cannot be disconnected.
- A disconnected graph does not have any spanning tree.



- > There are two methods are efficient:
 - 1. Kruskal's algorithm
 - 2. Prim's Algorithm

Kruskal's Algorithm:

- ▶ Kruskal's algorithm to find the minimum cost spanning tree uses the greedy approach.
- > This algorithm treats the graph as a forest and every node it has as an individual tree.
- A tree connects to another only and only if, it has the least cost among all available options and does not violate MST properties.
- > To understand Kruskal's algorithm let us consider the following example -



Step 1 - Remove all loops and Parallel Edges

➢ Remove all loops and parallel edges from the given graph.



Step 2 - Arrange all edges in their increasing order of weight

The next step is to create a set of edges and weight, and arrange them in an ascending order of weightage (cost).

B, D	D, T	A, C	C, D	С, В	В, Т	A, B	S, A	S, C
2	2	3	3	4	5	6	7	8

Step 3 - Add the edge which has the least weightage

- > Now we start adding edges to the graph beginning from the one which has the least weight.
- In case, by adding one edge, the spanning tree property does not hold then we shall consider not including the edge in the graph.



- ▶ The least cost is 2 and edges involved are B, D and D,T.
- We add them. Adding them does not violate spanning tree properties, so we continue to our next edge selection.
- ▶ Next cost is 3, and associated edges are A,C and C,D. We add them again -



▶ Next cost in the table is 4, and we observe that adding it will create a circuit in the graph. -



➤ We ignore it. In the process we shall ignore/avoid all edges that create a circuit.



- ▶ We observe that edges with cost 5 and 6 also create circuits.
- ➢ We ignore them and move on.



> Now we are left with only one node to be added.

▶ Between the two least cost edges available 7 and 8, we shall add the edge with cost 7.



➢ By adding edge S, A we have included all the nodes of the graph and we now have minimum cost spanning tree.

Prim's Algorithm:

- > Prim's algorithm to find minimum cost spanning tree.
- Prim's algorithm, treats the nodes as a single tree and keeps on adding new nodes to the spanning tree from the given graph.

Example -



Step 1 - Remove all loops and parallel edges



- ▶ Remove all loops and parallel edges from the given graph.
- ▶ In case of parallel edges, keep the one which has the least cost associated and remove all others.



Step 3 - Check outgoing edges and select the one with less cost

➢ After choosing the root node S, we see that S, A and S,C are two edges with weight 7 and 8, respectively. We choose the edge S, A as it is lesser than the other.



- ▶ Now, the tree S-7-A is treated as one node and we check for all edges going out from it
- \blacktriangleright We select the one which has the lowest cost and include it in the tree.



- After this step, S-7-A-3-C tree is formed. Now we'll again treat it as a node and will check all the edges again.
- ▶ However, we will choose only the least cost edge.
- ▶ In this case, C-3-D is the new edge, which is less than other edges' cost 8, 6, 4, etc.



- After adding node D to the spanning tree, we now have two edges going out of it having the same cost, i.e. D-2-T and D-2-B.
- \succ Thus, we can add either one.
- > But the next step will again yield edge 2 as the least cost.
- > Hence, we are showing a spanning tree with both edges included.



UNIT- IV	
Question Bank	
One word question and answers:	
1. How many children does a binary tree have?	
a) 2 b) any number of children c) 0 or 1 or 2 d) 0 or 1	Answer: c
2. What is/are the disadvantages of implementing tree using normal arrays?	
b) difficult in finding the parent of a node	
c) have to know the maximum number of nodes possible before creation of trees	5
d) difficult to implement	Answer: c
3. What must be the ideal size of array if the height of tree is '1'?	
a) 2l-1 b) l-1 c) 1 d) 2l	Answer: a
4. What are the children for node 'w' of a complete-binary tree in an array represen a) 2w and 2w+1 b) 2+w and 2-w c) w+1/2 and w/2 d) w-1/2 and w- Answer: a	+1/2
5. Advantages of linked list representation of binary trees over arrays?	
a) dynamic size b) ease of insertion/deletion c) ease in randomly acc	essing a node
d) both dynamic size and ease in insertion/deletion	Answer: d
6. 2. Disadvantages of linked list representation of binary trees over arrays?	
b) Extra memory for a pointer is needed with every element in the list	
c) Difficulty in deletion	
d) Random access is not possible and extra memory with every element	Answer: d
7. 2. Willish of the following terroring alogithm is not used to traverse in a travel	
a) Post order b) Pre order c) Post order d) Randomized	Answer: d
 8. 4. Level order traversal of a tree is formed with the help of a) breadth first search b) depth first search c) dijkstra's algorithm d) prim Answer: a 	s algorithm
9 5 Identify the reason which doesn't play a key role to use threaded binary trees?	
a) The storage required by stack and queue is more	
b) The pointers in most of nodes of a binary tree are NULL	
c) It is Difficult to find a successor node d) They occupy less size	Answer: d
10. What may be the psuedo code for finding the size of a tree?	
a) find_size(root_node->left_node) + 1 + find_size(root_node->right_node) b) find_size(root_node_>left_node) + find_size(root_node_>right_node)	
c) find size(root_node=>right_node) - 1	
d) find_size(root_node->left_node + 1	Answer: a
11. What is the maximum number of children that a binary tree node can have?	
a) $(0 \ b)$ $(1 \ c)$ $(2 \ d)$ $(3 \ c)$ 12 The following given tree is an example for?	Answer: c
12. The following given dee is an example for:	
(16) (12)	
a) Binary tree b) Binary search tree c) Fibonacci tree d) AVL tree	Answer: a
13. A binary tree is a rooted tree but not an ordered tree.	
a) true b) false Answer: b	
a) 1 b) 2 c) 3 d) 4 Answer: c	
15. What is the traversal strategy used in the binary tree?	
a) depth-first traversal b) breadth-first traversal c) random traversal d) Prior	rity traversal
Answer: b	

a) 1 b) 2 c) 3 d) 4	Answer: h
17. The average depth of a binary tree is given as?	
a) $O(N)$ b) $O(N)$ c) $O(N2)$ d) $O(\log N)$ 18. How many orders of traversal are applicable to a binary tree (In General)?	Answer: d
 a) 1 b) 4 c) 2 d) 3 19. If binary trees are represented in arrays, what formula can be used to locate a le has an index i? 	Answer: d ft child, if the node
a) $2i+1$ b) $2i+2$ c) $2i$ d) $4i$ 20 Using what formula can a parent node by located in an error?	Answer: a
a) $(i+1)/2$ b) $(i-1)/2$ c) $i/2$ d) $2i/2$	Answer: b
 21. Which of the following properties are obeyed by all three tree – traversals? a) Left subtrees are visited before right subtrees b) Right subtrees are visited before left subtrees c) Root node is visited before left subtree d) Root node is visited before right subtree 	Angwon o
22. The number of edges from the root to the node is called of the tree	Answer: a
a) Height b) Depth c) Length d) Width	Answer: b
23. The number of edges from the node to the deepest leaf is called of t	he tree.
a) Height b) Depth c) Length d) Width	Answer: a
24. What is a full binary tree?a) Each node has exactly zero or two children b) Each node has exactly two cc) All the leaves are at the same level d) Each node has exactly one or two ch	hildren ildren
	Answer: a
 a) Each node has exactly zero or two children b) A binary tree, which is completely filled, with the possible exception of the l is filled from right to left c) A binary tree, which is completely filled, with the possible exception of the l is filled from left to right 	oottom level, which oottom level, which
d) A tree In which all nodes have degree 2	Answer: c
26. What is the average case time complexity for finding the height of the binary tr a) $h = O(\log \log n)$ b) $h = O(n \log n) c$) $h = O(n)$ d) $h = O(\log n)$	ee? Answer: d
	Allower . u
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Uncomin a notepad Answer: d 	lo/Redo operations
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Unc in a notepad Answer: d 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 	lo/Redo operations e? Answer: b
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Unc in a notepad 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 29. In a full binary tree if number of internal nodes is I, then number of nodes N are a) N = 2*I b) N = I + 1 c) N = I - 1 d) N = 2*I + 1 	lo/Redo operations e? Answer: b e? Answer: d
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Uncentric in a notepad 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 29. In a full binary tree if number of internal nodes is I, then number of nodes N are a) N = 2*I b) N = I + 1 c) N = I - 1 d) N = 2*I + 1 30. In a full binary tree if there are L leaves, then total number of nodes N are? a) N = 2*L b) N = L + 1 c) N = L - 1 d) N = 2*L - 1 	lo/Redo operations e? Answer: b e? Answer: d Answer: d
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 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Unce in a notepad 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 29. In a full binary tree if number of internal nodes is I, then number of nodes N are a) N = 2*I b) N = I + 1 c) N = I - 1 d) N = 2*I + 1 d) N = 2*I + 1 e) N = L + 1 f) N = L + 1 f) N = L + 1 f) N = 2*L - 1 g) N = 2*L h) N = L + 1 h) N = L - 1 h) N = 2*L - 1 h) N = L + 1 h) N = 2*L - 1 h) N = 2*L - 1 h) Red-black tree c) Splay tree d) B-tree 32. Which of the following data structures can be efficiently implemented using he search tree?	lo/Redo operations e? Answer: b e? Answer: d Answer: d Answer: d eight balanced binary
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Uncertain a notepad 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 29. In a full binary tree if number of internal nodes is I, then number of nodes N are a) N = 2*I b) N = I + 1 c) N = I - 1 d) N = 2*I + 1 30. In a full binary tree if there are L leaves, then total number of nodes N are? a) N = 2*L b) N = L + 1 c) N = L - 1 d) N = 2*L - 1 31. Which of the following tree data structures is not a balanced binary tree? a) AVL tree b) Red-black tree c) Splay tree d) B-tree 32. Which of the following data structures can be efficiently implemented using he search tree? a) sets b) priority queue c) heap d) both sets and priority queue 	lo/Redo operations e? Answer: b e? Answer: d Answer: d Answer: d eight balanced binary Answer: d
 27. Which of the following is not an advantage of trees? a) Hierarchical structure b) Faster search c) Router algorithms d) Unce in a notepad 28. In a full binary tree if number of internal nodes is I, then number of leaves L are a) L = 2*I b) L = I + 1 c) L = I - 1 d) L = 2*I - 1 29. In a full binary tree if number of internal nodes is I, then number of nodes N are a) N = 2*I b) N = I + 1 c) N = I - 1 d) N = 2*I + 1 30. In a full binary tree if there are L leaves, then total number of nodes N are? a) N = 2*L b) N = L + 1 c) N = L - 1 d) N = 2*L - 1 31. Which of the following tree data structures is not a balanced binary tree? a) AVL tree b) Red-black tree c) Splay tree d) B-tree 32. Which of the following data structures can be efficiently implemented using he search tree? a) sets b) priority queue c) heap d) both sets and priority queue 33. Heap can be used as	lo/Redo operations e? Answer: b e? Answer: d Answer: d Eight balanced binary Answer: d mal Array Answer: a

35. What is the best case complexity in building a	heap?	
a) O(nlogn) b) O(n2) c) O(n*longn	*logn) d) O(n)	Answer: d
36. Which of the following statements for a simpl	e graph is correct?	
a) Every path is a trail b) Every trail i	is a path c) Every trail i	is a path as well as every path
is a trail d) Path and trail have 1	no relation	Answer: a
37. A graph with all vertices having equal degree	is known as a	—
a) Multi Graph b) Regular Graph c) Sim	iple Graph d) Co	mplete Graph
		Answer: b
Explanation: The given statement is the defini	tion of regular graphs.	
38. Which of the following ways can be used to re	epresent a graph?	
a) Adjacency List and Adjacency Matrix	b) Incidence Matrix	c) Adjacency List,
20 Space complexity for an adjacency list of an u	ndiracted graph having l	Answer: C
and E (edges) is	nuneeteu graph having i	arge values of v (vertices)
a) $O(E)$ b) $O(V*V)$ c) $O(E+V)$	d) $O(V)$	Answer: c
40. Time complexity to find if there is an edge bet	tween 2 particular vertice	es is
a) $O(V)$ b) $O(E)$ c) $O(1)$	d) O(V+E)	Answer: a
41. Which of the following is/are the operations per	formed by kruskal's algor	ithm.
i) sort the edges of G in increasing order by leng	th ii) keep a subgraph S o	f G initially empty iii) builds a
tree one vertex at a time		
A) i, and ii only B) ii and iii only	C) i and iii only	D) All i, ii and iii
42. Rather than build a subgraph one edge at a time		builds a tree one vertex at a
time.		
A) kruskal's algorithm B) prim's algorithm	C) dijkstra algorithm	D) bellman ford algorithm
43.3 is known as a greedy algorithm	n, because it chooses at ea	ch step the cheapest edge to
add to subgraph S.	~	
A) Kruskal's algorithm B) Prim's algorithm	C) Dijkstra algorithm	D) Bellman ford algorithm
44 The result of prim's algorithm is a total time hour	nd of	
A) $O(\log n)$ B) $O(m+n \log n)$ C) $O(t$	$D O(m \log n)$	
45. The process updates the costs	of all the vertices V, com	nected to a vertex U, if we
could improve the best estimate of the shortest p	ath to V by including (U,	V) in the path to V.
A) relaxation B) improvement C) sho	rtening D) Costing	-
46 turns out that one can find the sho	rtest paths from a given so	ource to all points in a graph in
the same time.		
A) Kruskal's algorithm B) Prim's algorithm	C) Dijkstra algorithm	D) Bellman ford algorithm
47 keeps two sets of vertices; S, the set	et of vertices whose shorte	est paths from the source have
already been determined and V-S, the remaining	y vertices.	
A) Kruskal's algorithm B) Prim's algorithm	C) Dijkstra algorithm	D) Bellman ford algorithm
48 is a more generalized single source	e shortest path algorithm	which can find the shortest
path in a graph with negative weighted edges.	O D'ilectre els suid se	
A) Kruskal's algorithm B) Phill's algorithm	c) Dijkstra algorithim	D) Bellman ford algorithm
49.A sample application of algorithm	is to solve chucai paul pi	oblem, i.e. midnig the longest
A) DAG application path algorithm B DA	G shortest nath algorithm	
C) DAG critical path algorithm D) Bel	llman ford algorithm	
	innun förd afgörtanni	
50. The floyd-warshall all pairs shortest path algorith	m computes the shortest r	baths between each pair of
nodes in	1 1	I.
A) $O(logn)$ B) $O(n^2)$ C) $O(mn)$	D) O(n^3)	
51.In a directed graph, the can compu	te the transitive hull in C	D(n^3)
A) Transitive Hull B) Minimax Distance	C) Max Min Distance	D) Safest Path

 52 means, for all vertices, compute a A) Transitive Hull B) Minimax Distance 53. For a directed graph with edge lengths, the floyd hetween each min of modes in O(nΔ2) 	its reachability. C) Max Min Distance D) Safest Path warshall algorithm can compute the
A) Transitive Hull B) Minimax Distance	C) Max Min Distance D) Safest Path
54.Given a directed graph where the edges are labele between the two nodes with floyd w	d with survival probabilities, we can compute the warshall.
A) Transitive Hull B) Minimax Distance	C) Max Min Distance D) Safest Path
 55 describe efficient algorithms for and adjacency matrix representations of G. A) Graph transpose problem C) Topological sort problem D) Euler path p 	r computing G^T from G, for both the adjacency list nected components problem roblem
56. In input is a directed acyclic graph ((DAG)G=(V,E).
 A) Graph transpose problem C) Topological sort problem 57. In, a directed graph G is acylic A) Graph transpose problem C) Topological sort problem C) Topological sort problem D) Euler path p 	nnected components problem problem c if and only if a DFS of G yields no back edge. nected components problem roblem
58 is a most generalized single source graph even with negative weights.	shortest path algorithm to find the shortest path in a
A) Kruskal's algorithm B) Prim's algorithm	C) Dijkstra algorithm D) Bellman ford algorithm
 59solves the problem of finding the A) Kruskal's algorithm B) Prim's algorithm 60. Dijkstra algorithm is also called the 	 ne shortest path from a point in a graph to a destination. C) Dijkstra algorithm D) Bellman ford algorithm
A) multiple source B) single source Answers	C) single destination D) multiple destination
1. A) i, and ii only	12. A) Transitive Hull
2. B) prim's algorithm	13. B) Minimax Distance
3. A) Kruskal's algorithm	14. D) Safest Path
4. B) O(m+n logn)	15. A) Graph transpose problem
5. A) relaxation	16. C) Topological sort problem
6. C) Dijkstra algorithm	17. C) Topological sort problem
7. C) Dijkstra algorithm 9. D) Ballman ford algorithm	18. D) Bellman ford algorithm
6. D) Bellman lord algorithm (0, R) DAC shortest path algorithm	19. C) Dijkstra algoritim 20. B) single source
10 D) $O(n^3)$	20. D) single source
11. A) Transitive Hull	
,	

5 Marks

- Explain in detail about types of trees.
 Write short notes on heap tree.
- Discuss in detail about tree terminologies.
 Write notes on graph terminologies.
- Give a detail note on minimum spanning tree.
 Write in detail about operations of tree.
- 7. Write in detail about operations of graphs.

10 Marks

- 1. What is Binary Tree? Explain Representation of Binary tree. Also explain different operation that can be performed on Binary tree.
- 2. Explain Inorder, Preorder and Postorder Traversal operation on Binary tree with example.
- 3. List the types of Binary Search Tree. Explain Insertion and Deletion Operation on Binary Search Tree with Example.
- 4. Explain in detail about red black tree with example.
- 5. Explain the various representation of graph with example in detail?
- 6. Explain Dijkstra's algorithm with an example?
- 7. Explain Prim's algorithm with an example?
- 8. Explain Krushal's algorithm with an example?

-----END------

UNIT – V

SEARCHING

What is searching?

- Searching is the process of finding a given value position in a list of values.
- > It decides whether a search key is present in the data or not.
- > It is the algorithmic process of finding a particular item in a collection of items.
- > It can be done on internal data structure or on external data structure.
- There are two types of search,
 - 1. Linear search
 - 2. Non-linear search

Searching Techniques

- > To search an element in a given array, it can be done in following ways.
 - 1. Sequential Search/Linear Search.
 - 2. Binary Search

1. Sequential Search/Linear Search

- Linear search is a very simple search algorithm.
- > In this type of search, a sequential search is made over all items one by one.
- Every item is checked and if a match is found then that particular item is returned, otherwise the search continues till the end of the data collection.



Fig. Sequential Search

i) Linear Search with Array:

Start the search from the first element and continue till you get the element (or reach end of the array).



Element to Search: 5

16	7	10	5	1	8	3	4	7	2
Î									

ii) Linear Search with linked list:

- > Our sequential search function for linked lists will take two arguments,
 - 1. A pointer to the first element in the list.
 - 2. The value for which we are searching.
- The function will return a pointer to the list structure containing the correct data, or will return NULL if the value wasn't found.

iii) Linear Search with ordered list:

- In order to implement the ordered list, we must remember that the relative positions of the items are based on some underlying characteristic.
- The ordered list of integers given above (17, 26, 31, 54, 77, and 93) can be represented by a linked structure as shown below.
- > Again, the node and link structure is ideal for representing the relative positioning of the items.



Fig. Working Structure of Binary Search

SORTING

What is sorting?

- Sorting refers to arranging data in a particular format. Sorting algorithm specifies the way to arrange data in a particular order.
- > Most common orders are in numerical or lexicographical order.
- The importance of sorting lies in the fact that data searching can be optimized to a very high level, if data is stored in a sorted manner.
- Sorting is also used to represent data in more readable formats.
- > Following are some of the examples of sorting in real-life scenarios –

Telephone Directory:

The telephone directory stores the telephone numbers of people sorted by their names, so that the names can be searched easily.

Dictionary:

> The dictionary stores words in an alphabetical order so that searching of any word becomes easy.

TERMINOLOGY:

What are Internal sorting?

When all data that needs to be sorted cannot be placed in-memory at a time, the sorting is called internal sorting.

What is External Sortings?

- > External Sorting is used for massive amount of data.
- > Merge Sort and its variations are typically used for external sorting.
- Some external storage like hard-disk, CD, etc is used for external storage. When all data is placed in-memory, then sorting is called internal sorting.

SORTING TECHNIQUES:

In-place Sorting

- Algorithms may require some extra space for comparison and temporary storage of few data elements.
- > These algorithms do not require any extra space and sorting is said to happen in-place.

Example: Bubble sort is an example of in-place sorting.

Not-in-place Sorting

- > Algorithms requires space which is more than or equal to the elements being sorted.
- Sorting which uses equal or more space is called not-in-place sorting.

Example: Merge-sort is an example of not-in-place sorting.

Stable Sorting:

➢ If a sorting algorithm, after sorting the contents, does not change the sequence of similar content in which they appear, it is called stable sorting.



Not Stable Sorting:

➢ If a sorting algorithm, after sorting the contents, changes the sequence of similar content in which they appear, it is called unstable sorting.



Adaptive Sorting Algorithm

- A sorting algorithm is said to be adaptive, if it takes advantage of already 'sorted' elements in the list that is to be sorted.
- That is, while sorting if the source list has some element already sorted, adaptive algorithms will take this into account and will try not to re-order them.

Non-Adaptive Sorting Algorithm

- ➤ A non-adaptive algorithm is one which does not take into account the elements which are already sorted.
- > They try to force every single element to be re-ordered to confirm their sortedness.

BUBBLE SORT

- ➢ Bubble sort is a simple sorting algorithm.
- This sorting algorithm is comparison-based algorithm in which each pair of adjacent elements is compared and the elements are swapped if they are not in order.
- This algorithm is not suitable for large data sets as its average and worst case complexities are of O (n2) where n is the number of items.

How Bubble Sort Works?

- > We take an unsorted array for our example.
- > Bubble sort takes O(n2) time so we're keeping it short and precise.



▶ Bubble sort starts with very first two elements, comparing them to check which one is greater.



In this case, value 33 is greater than 14, so it is already in sorted locations. Next, we compare 33 with 27.

14	33	27	35	10
----	----	----	----	----

We find that 27 is smaller than 33 and these two values must be swapped.

	\square	\square	\square	0
14	33	27	35	10

➤ The new array should look like this –

14 27	33	35	10	
-------	----	----	----	--

▶ Next we compare 33 and 35. We find that both are in already sorted positions.

14 27 33 35 10	
----------------	--

> Then we move to the next two values, 35 and 10.

➤ We know then that 10 is smaller 35. Hence they are not sorted.



- ➤ We swap these values.
- \succ We find that we have reached the end of the array.
- After one iteration, the array should look like this –

-	27	22	10	25
14	21	33		35

To be precise, we are now showing how an array should look like after each iteration. After the second iteration, it should look like this –

14	27	10	33	35
		\square		

> Notice that after each iteration, at least one value moves at the end.

14	10	27	33	35

And when there's no swap required, bubble sorts learns that an array is completely sorted.

10	14	27	33	35

▶ Now we should look into some practical aspects of bubble sort.

Algorithm

```
Begin BubbleSort (list)
for all elements of list
If list[i] > list [i+1]
Swap (list[i], list [i+1])
End if
End for
Return list
End Bubble Sort
```

INSERTION SORT

- > This is an in-place comparison-based sorting algorithm.
- ▶ Here, a sub-list is maintained which is always sorted.
- > For example, the lower part of an array is maintained to be sorted.
- An element which is to be 'inserted in this sorted sub-list, has to find its appropriate place and then it has to be inserted there.
- Hence the name, insertion sorts.
- The array is searched sequentially and unsorted items are moved and inserted into the sorted sub-list (in the same array).
- This algorithm is not suitable for large data sets as its average and worst case complexity are of O(n2), where n is the number of items.

How Insertion Sort Works?

➤ We take an unsorted array for our example.


14 10 27 33 35 19 42 44
> We swap them again. By the end of third iteration, we have a sorted sub-list of 4 items.
10 14 27 33 35 19 42 44
This process goes on until all the unsorted values are covered in a sorted sub-list.

- Now we shall see some programming aspects of insertion sort.

SELECTION SORT

- Selection sort is a simple sorting algorithm.
- > This sorting algorithm is an in-place comparison-based algorithm in which the list is divided into two parts, the sorted part at the left end and the unsorted part at the right end.
- ▶ Initially, the sorted part is empty and the unsorted part is the entire list.
- > The smallest element is selected from the unsorted array and swapped with the leftmost element, and that element becomes a part of the sorted array.
- > This process continues moving unsorted array boundary by one element to the right.
- This algorithm is not suitable for large data sets as its average and worst case complexities are of O (n2), where n is the number of items.

How Selection Sort Works?

> Consider the following depicted array as an example.

14	33	27	10	35	19	42	44
				\square			

> For the first position in the sorted list, the whole list is scanned sequentially. The first position where 14 is stored presently, we search the whole list and find that 10 is the lowest value.

(14	33	27	10	35	19	42	44
Ĺ	\square	\square	\square		\square	\square	\square	\square

> So we replace 14 with 10. After one iteration 10, which happens to be the minimum value in the list, appears in the first position of the sorted list.

	\square	\square	\square		\square	\square	
10	33	27	14	35	19	42	44

> For the second position, where 33 is residing, we start scanning the rest of the list in a linear manner.



> We find that 14 is the second lowest value in the list and it should appear at the second place. We swap these values.

10	33	27	14	35	19	42	44
----	----	----	----	----	----	----	----

> After two iterations, two least values are positioned at the beginning in a sorted manner.

	10	14	27	33	35	19	42	44
L								

- \blacktriangleright The same process is applied to the rest of the items in the array.
- ➢ Following is a pictorial depiction of the entire sorting process −

MERGE SORT

- > Merge sort is a sorting technique based on divide and conquer technique.
- \blacktriangleright With worst-case time complexity being O(n log n), it is one of the most respected algorithms.
- > Merge sort first divides the array into equal halves and then combines them in a sorted manner.

How Merge Sort Works?

> To understand merge sort, we take an unsorted array as the following –

14 33 27 10 35 19 42 44
> We know that merge sort first divides the whole array iteratively into equal halves unless the atomic
values are achieved.
> We see here that an array of 8 items is divided into two arrays of size 4.
14 33 27 10 35 19 42 44
> This does not change the sequence of appearance of items in the original.
\blacktriangleright Now we divide these two arrays into halves.
14 33 27 10 35 19 42 44
> We further divide these arrays and we achieve atomic value which can no more be divided.
14 33 27 10 35 19 42 44
Now, we combine them in exactly the same manner as they were broken down. Please note the
color codes given to these lists
We first compare the element for each list and then combine them into another list in a sorted
manner.
➢ We see that 14 and 33 are in sorted positions.
➢ We compare 27 and 10 and in the target list of 2 values we put 10 first, followed by 27.
\blacktriangleright We change the order of 19 and 35 whereas 42 and 44 are placed sequentially.
14 33 10 27 19 35 42 44
> In the next iteration of the combining phase, we compare lists of two data values, and merge them
into a list of found data values placing all in a sorted order.
10 14 27 33 19 35 42 44
After the final marging, the list should look like this –
After the final merging, the fist should look like this
10 14 19 27 33 35 42 44
> Now we should learn some programming aspects of merge sorting.
s and the should reach bolic programming appeels of merge borting.

QUICK SORT

- Quick sort is a highly efficient sorting algorithm and is based on partitioning of array of data into smaller arrays.
- A large array is partitioned into two arrays one of which holds values smaller than the specified value, say pivot, based on which the partition is made and another array holds values greater than the pivot value.
- > Quick sort partitions an array and then calls itself recursively twice to sort the two resulting subarrays.

Partition in Quick Sort

> Following animated representation explains how to find the pivot value in an array.

Unsorted Array



> The pivot value divides the list into two parts. And recursively, we find the pivot for each sub-lists



until all lists contains only one element.

➢ Now, let us learn some programming aspects of selection sort.

HEAP SORT

- ▶ Heap sort is a comparison based sorting algorithm.
- ➢ It is a special tree-based data structure.
- Heap sort is similar to selection sort. The only difference is, it finds largest element and places it at the end.
- > This sort is not a stable sort. It requires a constant space for sorting a list.
- It is very fast and widely used for sorting.
- It has following two properties:
 - 1. Shape Property
 - 2. Heap Property

Shape Property

Shape property represents all the nodes or levels of the tree are fully filled.



Heap property

- ▶ Heap property is a binary tree with special characteristics.
- It can be classified into two types,

- 1. Max-Heap.
- 2. Min Heap.

<u>Max Heap</u>:

> If the parent nodes are greater than their child nodes, it is called a Max-Heap. <u>*Min Heap:*</u>

> If the parent nodes are smaller than their child nodes, it is called a Min-Heap



UNIT- V Question Bank

One word question and answers:

one wo	ord question and answers:	
1.	Is there any difference in the speed of execution between linear serach(recursive)	vs linear
	search(lterative)?	
	a) Both execute at same speed b) Linear search(recursive) is faster	
	c) Linear search(Iterative) is faster d) Cant be said	Answer: c
2.	Is the space consumed by the linear search(recursive) and linear sear	ch(iterative) same?
	a) No, recursive algorithm consumes more space b) No, recursive algorithm consumes	umes less space c)
_	Yes d) Nothing can be said	Answer: a
3.	What is the worst case runtime of linear search(recursive) algorithm?	
	a) $O(n)$ b) $O(logn)$ c) $O(n2)$ d) $O(nx)$	Answer: a
4.	Linear search(recursive) algorithm used in	
	a) When the size of the dataset is low b) When the size of the dataset is large	
_	c) When the dataset is unordered d) Never used	Answer: a
5.	What is the best case runtime of linear search (recursive) algorithm on an ordered (1)	set of elements?
	a) $O(1)$ b) $O(n)$ c) $O(logn)$ d) $O(nx)$	Answer: a
6.	What is the recurrence relation for the linear search recursive algorithm? $M(-2) = M(-1) = M$	
_	a) $\Gamma(n-2)+c$ b) $2\Gamma(n-1)+c$ c) $\Gamma(n-1)+c$ d) $\Gamma(n+1)+c$	Answer: c
7.	What is the worst case complexity of binary search using recursion?	
0	a) $O(nlogn)$ b) $O(logn)$ c) $O(n)$ d) $O(n2)$	Answer: D
8.	what is the average case time complexity of binary search using recursion?	A h
0	a) O(nogn) b) O(logn) c) O(n) d) O(n2)	Answer: D
9.	what is the time complexity of binary search with heration? $a) O(r) = a + b) O(logr) = a) O(r) = d) O(r^2)$	A namon h
10	$\begin{array}{c} a) O(110g11) & b) O(10g11) & c) O(11) & d) O(112) \\ How many passes does an insertion sort algorithm consist of? \\ \end{array}$	Allswer: D
10.	a) N b) N 1 c) N 1 d) N2	Answer: h
	a) N 0) N-1 C) N+1 0) N2 Explanation: An insertion algorithm consists of N 1 passes when an array of N al	Allswel. D
11	2 Which of the following algorithm implementations is similar to that of an inset	rtion sort?
11.	a) Binary heap b) Quick sort c) Merge sort d) Radix sort	Answer a
	Explanation: Insertion sort is similar to that of a binary heap algorithm because of	f the use of
	temporary variable to swap	
12.	3. What is the average case running time of an insertion sort algorithm?	
	a) $O(N)$ b) $O(N \log N)$ c) $O(\log N)$ d) $O(N2)$	Answer: d
13.	Which of the following real time examples is based on insertion sort?	
	a) arranging a pack of playing cards b) database scenarios and distributes sce	narios
	c) arranging books on a library shelf d) real-time systems	Answer: a
14.	Which of the following sorting algorithms is the fastest for sorting small arrays?	
	a) Quick sort b) Insertion sort c) Shell sort d) Heap sort	Answer: b
15.	For the best case input, the running time of an insertion sort algorithm is?	
	a) Linear b) Binary c) Quadratic d) Depends on the input	Answer:
16.	Which of the following examples represent the worst case input for an insertion s	ort?
	a) array in sorted order b) array sorted in reverse order c) normal unsorted array	У
	d) large array	Answer: b
17.	Which of the following sorting algorithm is best suited if the elements are already	y sorted?
	a) Heap Sort b) Quick Sort c) Insertion Sort d) Merge Sort	Answer: c
18.	Which of the following is not an exchange sort?	
	a) Bubble Sort b) Quick Sort c) Partition-exchange Sort d) Insertion Sort	Answer: d
19.	What is an external sorting algorithm?	
	a) Algorithm that uses tape or disk during the sort	
	b) Algorithm that uses main memory during the sort	
	c) Algorithm that involves swapping d) Algorithm that are considered 'in place	ce' Answer: a
20.	What is an internal sorting algorithm?	· · · · · · · · · · · · · · · · · · ·
	a) Algorithm that uses tape or disk during the sort b) Algorithm that uses r	nain memory

during the sort

c) Algorithm that involves swapping d) Algorithm that are considered 'in place' **Answer: b** 21. What is the average case complexity of bubble sort?

- a) O(nlogn)b) O(logn)c) O(n)d) O(n2)Answer: d22. Merge sort uses which of the following technique to implement sorting?
- a) backtracking b) greedy algorithm c) divide and conquer d) dynamic programming **Answer: c**
- 23. Which of the following is not in place sorting algorithm?
 - a) merge sort b) quick sort c) heap sort d) insertion sort

Answer: a

- 24. Which of the following stable sorting algorithm takes the least time when applied to an almost sorted array?
 - a) Quick sort b) Insertion sort c) Selection sort d) Merge sort Answer: d

25. Which of the following sorting algorithm makes use of merge sort?a) tim sortb) intro sortc) bogo sortd) quick sortAnswer: a

5 Marks

- 1. Write notes on linear searching algorithm.
- 2. Explain about binary tree searching.
- 3. Write about sorting terminology.
- 4. Discuss about quick sort.
- 5. Write an algorithm of selection sort.

10 Marks

- 1. Write notes on linear searching techniques.
- 2. Write notes on bubble sort with example.
- 3. Discuss in detail about merge sort with example.
- 4. Write in detail about non linear searching.
- 5. Discuss about unordered list.

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